

**Table S1. Standardized Nomenclature for Mouse Embryo Staging, Related to Figure 1**

<b>Neural tube time (hph; hours post headfold stage)</b>	<b>Embryonic day</b>	<b>Number of somites</b>
0hph	E7.5	0 (headfold stage)
8hph	E8.0	3-4
18hph	E8.4	8-9
20hph	E8.5	10-11
40hph	E8.75	20-22
50hph	E9.0	25-27
60hph	E9.5	30-32
70hph	E10.0	35-37
80hph	E10.5	40
90hph	E11.0	NA
100hph	E11.5	NA

**Table S2. Set of Parameter Values Generating the Relevant Biological Outputs,  
Related to Figure 4  
(Initial value for P =3)**

<b>Parameters</b>	<b>Description</b>	<b>Value</b>
$\alpha$	Maximum rate of P	3
$\beta$	Maximum rate of O	5
$\gamma$	Maximum rate of N	5
$h_1$	Strength of N repression on P	6
$h_2$	Strength of O repression on P	2
$h_3$	Strength of N repression on O	5
$h_4$	Strength of O repression on N	1
$h_5$	Strength of P repression on N	1
$k_1$	Rate of P degradation	1
$k_2$	Rate of O degradation	1
$k_3$	Rate of N degradation	1
$O_{critP}$	Critical value of O for which P value has reached half of its maximal	1
$N_{critP}$	Critical value of N for which P value has reached half of its maximal	1
$O_{critN}$	Critical value of O for which N value has reached half of its maximal	1
$N_{critO}$	Critical value of N for which O value has reached half of its maximal	1
$P_{critN}$	Critical value of P for which N value has reached half of its maximal	1
$n$	Hill coefficient of G cooperativity on O	1
$m$	Hill coefficient of G cooperativity on N	1

**Table S3. Identification of the Parameters Robust or Sensitive to a 2-Fold Increase or Decrease in Their Values, Related to Figure 4**

The tick marks indicate the parameter changes for which the system adopts the biological relevant outputs over time or when G is increased, as well as in conditions where P or O were removed ( $\alpha$  or  $\beta=0$ , respectively). A, B, C, D indicate that the system fails to adopt the biological relevant output when the parameter is changed. In failure A, the system adopts an  $O^{\text{HIGH}}$  state for all values of G above a certain threshold and N is never induced. B indicates that in the absence of O, P prevails for all values of G and N is never induced. P, O and N coexist even at high values of G in Failure C. In Failure D, O is not induced for any value of G.

<b>Parameters</b>	<b>Value doubled</b>	<b>Value halved</b>
$\alpha$	✓	✓
$\beta$	A	✓
$\gamma$	✓	A,B
$h_1$	✓	✓
$h_2$	✓	✓
$h_3$	✓	✓
$h_4$	A	✓
$h_5$	B	✓
$k_1$	✓	B
$k_2$	✓	A
$k_3$	A,B	✓
$N_{critP}$	C,B	✓
$O_{critP}$	✓	✓
$N_{critO}$	A	D
$O_{critN}$	✓	A
$P_{critN}$	✓	✓
$n$	✓	✓
$m$	✓	✓