1 Modeling the effect of vaccination on selection for antibiotic resistance in S. 2 pneumoniae 3 4 Nicholas G. Davies^{1*}, Stefan Flasche¹, Mark Jit^{1,2}, Katherine E. Atkins^{1,3} 5 6 1. Centre for Mathematical Modelling of Infectious Diseases; Vaccine Centre; and 7 Department of Infectious Disease Epidemiology, London School of Hygiene and Tropical 8 Medicine, London, UK. 9 2. Modelling and Economics Unit, Public Health England, London, UK. 10 3. Centre for Global Health, Usher Institute of Population Health Sciences and 11 Informatics, The University of Edinburgh, Edinburgh, UK. 12 * Corresponding author E-mail: nicholas.davies@lshtm.ac.uk. 13 14 15 16 **Overline: Bacterial infections** 17 18 **One sentence summary:** Bacterial competition and diversity may influence selection 19 for antibiotic-resistant bacteria after vaccination. 20 21 22 **Accessible Summary:** 23 Using mathematical modelling, we show that the association between penicillin 24 consumption and penicillin non-susceptibility in *Streptococcus pneumoniae* across 27 25 European countries can be explained by four different models of antibiotic resistance 26 evolution, out of nine potential models we identified by searching the literature. Each 27 model encapsulates an alternative hypothesis for why antibiotic-sensitive and 28 antibiotic-resistant bacterial strains coexist in the same population. We show that, 29 depending upon the model, vaccination can either inhibit or promote the spread of 30 antibiotic resistance. Our work suggests testable hypotheses to help predict or explain changes in antibiotic resistance following the introduction of new vaccines. 31

Abstract

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

48

49

50

51

52

53

54

56

57

58

59

60

61

62

63

64

Vaccines against bacterial pathogens can protect recipients from becoming infected with potentially antibiotic-resistant pathogens. But by altering the selective balance between antibiotic sensitive and resistant bacterial strains, vaccines may also suppress—or spread—antibiotic resistance among unvaccinated individuals. Predicting the outcome of vaccination requires knowing what drives selection for drug-resistant bacterial pathogens and what maintains the circulation of both antibiotic-sensitive and antibiotic-resistant strains of bacteria. Using mathematical modeling and data from 2007 on penicillin consumption and penicillin non-susceptibility in *S. pneumoniae* invasive isolates from 27 European countries, we show that the frequency of penicillin resistance in *Streptococcus pneumoniae* (pneumococcus) can be explained by betweenhost diversity in antibiotic use, heritable diversity in pneumococcal carriage duration, or frequency-dependent selection brought about by within-host competition between antibiotic-resistant and sensitive *S. pneumoniae* strains. We used our calibrated models to predict the impact of non-serotype-specific pneumococcal vaccination upon the prevalence of *S. pneumoniae* carriage, incidence of disease, and frequency of *S.* pneumoniae antibiotic resistance. We found that the relative strength and directionality of competition between drug resistant and sensitive pneumococcal strains was the most important determinant of whether vaccination would promote, inhibit, or have little effect upon the evolution of antibiotic resistance. Finally, we show that country-specific differences in pathogen transmission substantially altered the predicted impact of vaccination, highlighting that policies for managing antibiotic resistance with vaccines must be tailored to a specific pathogen and setting.

55

Introduction

In an age of widespread antibiotic resistance, there is growing interest in using vaccines to prevent bacterial infections that would otherwise call for treatment with antibiotics (1-4). This interest arises for two main reasons: first, vaccines are effective against both antibiotic-resistant and antibiotic-sensitive bacteria; and second, successful prophylaxis removes the need for a course of antibiotic therapy that might promote more resistance (2-5). Over the past two decades, the use of pneumococcal conjugate vaccines has seemingly borne out these advantages. Administering pneumococcal conjugate vaccines to young children has substantially reduced disease caused by *S. pneumoniae* (5-8)—a

common asymptomatic bacterial coloniser of the nasopharynx that can cause pneumonia, meningitis and other infections when invasive. Administration of pneumococcal conjugate vaccines has decreased demand for antibiotic therapy, largely by reducing cases of otitis media (5, 9). But because pneumococcal conjugate vaccine formulations target only a fraction of the \sim 100 known pneumococcal serotypes, the niche vacated by vaccine-targeted serotypes has been filled by non-vaccine serotypes, and overall pneumococcal carriage has rebounded to pre-vaccine levels (10, 11). Concomitantly, the incidence of infections attributed to *S. pneumoniae* non-vaccine serotypes (12) and the proportion of non-vaccine-type infections exhibiting antibiotic resistance (5, 13) have increased in many settings. Concern over serotype replacement, along with the high cost of manufacturing pneumococcal conjugate vaccines, has spurred the development of "universal" (non-serotype-specific) whole-cell or proteinbased pneumococcal vaccines protecting against all pneumococcal serotypes, some of which are now in early-stage clinical trials (14). If successful, universal pneumococcal vaccines could reduce the burden of pneumococcal disease without selecting for serotype replacement.

It remains unclear, however, how universal vaccination itself may impact the evolution of antibiotic resistance in *S. pneumoniae*, which is a concern given that vaccination is unlikely to eliminate pneumococcal carriage entirely (15). Mathematical models of bacterial transmission can be used to predict the impact of vaccination on antibiotic resistance (16, 17), but existing models for *S. pneumoniae* focus on serotype-specific vaccines and, even then, disagree over the expected impact of vaccination on resistance evolution (18–24). Comparing and interpreting the results of these models is hampered by the fact that none starts from a position of recapitulating large-scale empirical patterns of antibiotic resistance. The main challenge in replicating these patterns lies in identifying the mechanisms that maintain long-term coexistence between antibiotic-sensitive and antibiotic-resistant pneumococcal strains across a wide range of antibiotic treatment rates, like those seen across Europe and the United States (25, 26). Robust predictions of the long-term impact of non-serotype-specific vaccination on drug-resistant pneumococcal disease require a mechanistic understanding of these patterns.

Results

99

98

100 Stability in antibiotic resistance evolution can be maintained by frequency-101 dependent competition or extrinsically-imposed diversity. 102 A mathematical model must be able to explain the current burden of an infectious 103 disease before it can be used to robustly predict the impact of interventions for 104 managing that disease. Across Europe, the frequency of antibiotic resistance among 105 isolates from pneumococcal infections shows two salient features for models to 106 recapitulate (Fig. S1). One feature is spatial: the frequency of penicillin non-107 susceptibility varies between countries, and is higher in countries where more penicillin 108 is consumed (27). The other is temporal: although in individual countries, resistance 109 fluctuates from year to year, the overall frequency across Europe of penicillin non-110 susceptibility in pneumococcal isolates has remained steady at roughly 12% since 111 consolidated records began in 2005 (28). These observations contradict simple models 112 of antibiotic resistance evolution, which predict that intermediate frequencies of 113 resistance cannot be stably maintained in the long term: that is, either sensitive strains 114 will competitively exclude resistant strains, or resistant strains will competitively 115 exclude sensitive strains, unless there is some mechanism that maintains coexistence 116 between them (25, 29). 117 118 By conducting a literature search, we identified nine such potential mechanisms (25, 26, 119 30–41) that fall into two broad classes. In one class, coexistence is maintained by 120 environmental or genetic diversity that effectively creates separate niches for resistant 121 and sensitive strains, preventing them from completely overlapping in competition. In 122 the other class, competition between resistant and sensitive strains is itself the 123 stabilising factor that maintains coexistence, because resistant and sensitive strains 124 exhibit alternative competitive phenotypes that afford strains a competitive advantage when rare, thus promoting negative frequency-dependent selection for antibiotic 125 126 resistance. Thus, extrinsically-imposed diversity and frequency-dependent competition 127 are two key forces maintaining stability in antibiotic resistance evolution. We suggest 128 that four of the nine identified mechanisms for maintaining coexistence are biologically 129 plausible for *S. pneumoniae* (Table 1).

Four models of antibiotic resistance evolution. To compare these four mechanisms, we embedded each in a shared model framework of person-to-person transmission of nasopharyngeal pneumococcal carriage. This framework tracks the country-specific frequency of resistance in pneumococci circulating among children under five years old, the age group that drives the majority of pneumococcal transmission and disease (42, 43). We assume that each individual makes effective contact with another random individual at rate β , thereby potentially acquiring a strain (either sensitive or resistant) carried by the contacted person. With probability *c*, resistant strains fail to transmit, where *c* represents the transmission cost of resistance (44, 45). A carrier naturally clears all strains at rate u, and is exposed to antibiotic therapy at a country-specific rate τ , which clears the host of sensitive strains only. We assumed this treatment rate is independent of carriage status (46) and we did not explicitly track disease progression in hosts. Under the "Treatment diversity" and "Pathogen diversity" models, extrinsicallymaintained diversity among hosts or among pathogens prevents competitive exclusion by keeping antibiotic-resistant and sensitive strains from fully competing with each other. In the "Treatment diversity" model (Fig. 1A), heterogeneity in the consumption of antibiotics between host subpopulations within a country maintains coexistence (25, 34, 35). These subpopulations could correspond to geographical regions, socioeconomic strata, host age and risk classes, or a combination of these. Provided that transmission between high-consumption (resistance-promoting) and low-consumption (resistanceinhibiting) subpopulations is not too frequent, an intermediate frequency of resistance can be maintained across the whole population. Because coexistence is maintained by assortative mixing between subpopulations differing in antibiotic use, the key parameters governing coexistence in this model are κ, the variability in antibiotic consumption between subpopulations, and g, the relative rate at which within-country contact is made within subpopulations rather than between them (Fig. S2). In the "Pathogen diversity" model (Fig. 1B), pneumococci are divided into subtypes ("Dtypes") (38) that vary in their mean duration of natural carriage. All else being equal, the D-type with the longest carriage duration would be expected to competitively exclude all other strains; the model assumes that diversifying selection acting on the D-

131

132

133

134

135

136

137

138

139

140

141

142

143

144

145

146

147

148

149

150

151

152

153

154

155

156

157

158

159

160

161

162

type locus keeps all subtypes in circulation. What D-types correspond to is not explicitly specified by this model, but one candidate is serotype variation. For example, if antigenic diversity is promoted by host acquired immunity to capsular serotypes, and serotypes tend to differ in their intrinsic ability to evade clearance by the immune system, then intermediate resistance can be maintained because selection for resistance tends to be greater in serotypes that have a longer duration of carriage (38). Longlasting serotypes will tend to evolve resistance, while shorter-lived serotypes will tend not to—a pattern observed in *S. pneumoniae* (38) and reproduced by this model (Fig. S3). The parameters governing coexistence in this model are a, the strength of diversifying selection on the D-type locus, and δ , the variability between subtypes in clearance rate.

Under the "Treatment competition" and "Growth competition" models, coexistence is maintained by within-host competition between sensitive and resistant strains. In these models, hosts can be co-colonised by multiple strains. Then, competition between strains within the host niche determines which strain is transmitted to other potential hosts (26). The "Treatment competition" model (Fig. 1C) assumes that antibiotic therapy mediates within-host competition, such that when a co-colonised host takes antibiotics (i.e., at rate τ), the sensitive strains are cleared and only the resistant strains are transmitted to other hosts. The "Growth competition" model (Fig. 1D) has both treatment-mediated and growth-mediated competition: in the presence of antibiotics, resistant strains still outcompete co-colonising sensitive strains, whereas in the absence of antibiotics, sensitive strains gradually outcompete co-colonising resistant strains at rate *b*. We assumed that there is no transmission cost of resistance in this latter model (i.e., c = 0); instead, the within-host growth advantage b of sensitive strains accounts for the cost of resistance. In these competition models, resistant strains have an advantage in antibiotic-mediated competition, and sensitive strains have an advantage in growthmediated competition. These alternative forms of within-host competition can both promote coexistence because rare strains can more consistently exploit a competitive advantage over common strains, thus creating negative frequency-dependent selection for resistance (26). The key parameter governing coexistence in these two models is k, the relative rate of co-colonisation compared to primary colonisation.

In all four models, we assume that contact between individuals is assortative by country, such that with probability f, contact is with a random person from the same country, and with probability 1 - f, contact is with a random person from any country. We implement these models using systems of ordinary differential equations. All four models (25, 26, 38) are structurally neutral (25, 29), meaning that any coexistence exhibited by the models is accounted for by the specified biological mechanism rather than by any bias in the logical structure of the model that generates coexistence "for free" (29). Additionally, whereas the within-host competition models capture cocolonisation using a simplified subset of only 2 "mixed-carriage" states (S_R and R_S , Fig. 1A, B), we have previously shown (26) that this is equivalent to a more complex individual-based model with an arbitrary number of mixed-carriage states.

All four models reproduce observed patterns of antibiotic resistance.

The European Centre for Disease Prevention and Control (ECDC) monitors antibiotic consumption and resistance evolution across European countries (13, 28). These data capture a natural experiment in resistance evolution: for each monitored drug and pathogen, each country reports a different rate of antibiotic consumption in the community and exhibits a different frequency of resistance among invasive bacterial isolates. By fitting models to this multi-country data set, we can potentially rule out models that cannot reproduce the large-scale patterns that are observed. We used Bayesian inference to fit the model-predicted equilibrium frequency of resistance to the reported frequency of penicillin non-susceptibility in S. p pneumoniae across 27 European countries, assuming a 50% carriage prevalence (11, 42) and a carriage duration of 47 days (47, 48) in children under five years old. We began by assuming that countries only differ by their reported treatment rate—where we define a treatment course as equivalent to z = 5 defined daily doses of penicillin—with other model parameters shared across countries.

Strikingly, each model fits equally well to the empirical relationship between resistance and antibiotic use (Widely Applicable Information Criteria are similar across all models; Fig. 2A) and recovers plausible posterior parameter distributions (Fig. 2B; Fig. S4). That is, the empirical data do not distinguish between the four alternative mechanisms of resistance evolution we have identified. Later, we relax the assumption that only the

230 treatment rate varies between countries, allowing us to capture additional between-231 country variation in antibiotic resistance not explained by population-wide penicillin 232 consumption. 233 234 Mechanisms of resistance evolution determine the impact of vaccination on 235 antibiotic-resistant disease. 236 To determine the impact of universal vaccination on pneumococcal disease, we 237 considered three outcomes. The first is the impact of the vaccine upon the prevalence of 238 pneumococcal carriage. The second is the vaccine impact upon the frequency of 239 penicillin resistance among circulating pneumococcal strains remaining after 240 vaccination. The third is the impact of the vaccine upon the prevalence of antibiotic-241 resistant pneumococcal carriage—*i.e.*, the prevalence of carriage multiplied by the 242 frequency of penicillin resistance. Given that all four models are equally capable of 243 recapitulating observed patterns of penicillin resistance in *S. pneumoniae*, our aim was 244 to determine whether the mechanism maintaining stability in antibiotic resistance 245 evolution—frequency-dependent competition or extrinsically-imposed diversity— 246 matters when forecasting the impact of interventions for managing antibiotic 247 resistance. 248 249 We consider two alternative non-serotype-specific vaccines: an "acquisition-blocking" 250 vaccine, which prevents carriage from being established with probability ε_a , and a 251 "clearance-accelerating" vaccine, which shortens the duration of carriage by a fraction 252 ε_c . Both vaccines reduce pneumococcal transmission through alternative modes of host 253 immunity that might be elicited by a whole-cell or protein-based universal 254 pneumococcal vaccine. Analogously to naturally-acquired serotype-independent 255 pneumococcal immunity (49), the protective effect of whole-cell vaccines manifests as 256 accelerated clearance (50); it is unclear whether protein-based vaccines would block 257 pneumococcal acquisition—as pneumococcal conjugate vaccines do—or accelerate 258 clearance as whole-cell vaccines do (51). We refer to ε_a or ε_c as the vaccine efficacy, and 259 for simplicity, we assume that all children under five years old have vaccine protection, 260 as would be established by an infant vaccination programme rolled out across Europe.

In order to compare these vaccines with an alternative intervention of antibiotic

stewardship, we also evaluated the impact of reducing the rate of penicillin prescribing by a fraction ϵ_s .

We found that both vaccines have a similar impact upon pneumococcal carriage prevalence, regardless of whether competition or diversity maintains stability in resistance evolution (Fig. 3A). Specifically, as the vaccine efficacy ϵ_a or ϵ_c increases, carriage decreases, with the elimination of pneumococcal carriage occurring at a vaccine efficacy between 50 and 60%. Reducing antibiotic prescribing moderately increases pneumococcal carriage, such that carriage prevalence increases to approximately 54% across all countries when penicillin prescribing is eliminated completely.

The mechanism of resistance evolution, however, has a substantial impact upon whether vaccines increase or decrease the frequency of antibiotic resistance in *S.* pneumoniae in the long term (Fig. 3B). In the "Treatment diversity" and "Pathogen diversity" models, the acquisition-blocking vaccine has relatively little impact upon the frequency of resistance, because administering a universal pneumococcal vaccine to all individuals does not substantially alter the distribution of antibiotic use or of heritable variation in clearance rates. By contrast, in the within-host competition models, vaccination has a substantial impact upon resistance evolution because by reducing pneumococcal circulation, vaccines decrease the rate at which strains encounter each other within hosts, and hence strongly decrease competition between pneumococcal strains. Specifically, the acquisition-blocking vaccine selects strongly against resistance in the "Treatment competition" model: given that antibiotic-mediated within-host competition benefits the resistant strain in this model, the vaccine works against this competitive advantage and therefore inhibits antibiotic resistance. Conversely, in the "Growth competition" model, growth-mediated competition benefits the sensitive strain, and so by reducing competition, vaccination tends to promote antibiotic resistance. These results expand upon our previous finding that the rate of cocolonisation modulates antibiotic resistance evolution through its impact upon withinhost competition (26).

The clearance-accelerating vaccine exhibits similarly divergent impacts across mechanisms of antibiotic resistance evolution. However, compared with the acquisition-blocking vaccine, it also has an additional resistance-inhibiting effect across all models, because a shorter duration of carriage—whether natural or vaccine-induced—selects against resistance (38). This suggests that vaccines that accelerate natural clearance have a particular potential for managing antibiotic-resistant infections. As expected, reducing the rate of penicillin prescribing selects against resistance, exhibiting a similar impact across all four models.

The impact on antibiotic-resistant pneumococcal carriage (Fig. 3C), which combines changes in the prevalence of carriage and changes in the frequency of resistance, can be treated as a proxy for the incidence of antibiotic-resistant infections. Overall, under the "Growth competition" model, vaccination at intermediate efficacy is expected to increase the rate of antibiotic-resistant carriage, and hence the number of cases of resistant disease. In other models, vaccination always reduces resistant carriage, particularly under the "Treatment competition" model. A summary of the strongest vaccine impacts is shown in Fig. 3D.

Evidence to inform health policy and vaccine clinical trials.

For vaccines to be considered an efficient means of controlling antibiotic-resistant bacterial infections, they must compare favourably to existing interventions, such as reducing inappropriate antibiotic use (52). The UK government has recently announced an initiative to reduce antibiotic consumption by 15% by the year 2024 (52). Our models predict that a 15% reduction in primary-care penicillin consumption would reduce carriage of penicillin-non-susceptible pneumococci from 6% to 3%. The vaccine efficacy required to yield the same effect varies considerably depending upon the mechanism of antibiotic resistance evolution (Fig 4A); for example, the required vaccine efficacy is lowest under the "Treatment competition" model (ϵ_a = 11% or ϵ_c = 7%), and highest under the "Growth competition" model (ϵ_a = 52% or ϵ_c = 50%). A full comparison of vaccine and antibiotic stewardship interventions would require accounting for the economic cost of vaccines versus antibiotics, the wider range of antibiotic-resistant pathogens that would be targeted by restrictions on antibiotic use,

and any potential increase in pathogen circulation that might be brought about by inadvertent decreases in appropriate antibiotic use.

In randomized controlled clinical trials of pneumococcal vaccines, antibiotic resistance-related endpoints have routinely been evaluated over a follow-up period of between 6 months and 3.5 years after vaccination (53, 54). If vaccine-induced changes in resistance evolution unfold over a considerably longer timescale, similarly-designed trials may not fully capture vaccine impact on antibiotic resistance. Indeed, we found that it can take 5–10 years for antibiotic resistance to stabilise following vaccination (Fig. 4B), and that short-term drops in resistance can be reversed—or even give way to increased resistance—in the long term. Moreover, a trial in which vaccination is not offered to a substantial fraction of the population would not capture the full impact of reduced pneumococcal circulation, which is what drives competition-mediated changes in resistance in our models. Finally, our analysis assumes that vaccines are administered to all recipients simultaneously. In the real world, where vaccination is likely to be rolled out gradually, the full effect of vaccination would take even longer to observe.

The impact of vaccination at a national level varies depending upon the antibiotic treatment rate in a given country. Focusing on the specific outcome of childhood pneumococcal pneumonia cases, we found that while interventions have a consistent impact from country to country on the total pneumonia case rate, the impact on antibiotic-resistant pneumonia cases is greatest in those countries where antibiotic use, and hence resistance, is highest (Fig. 4C). We focused on antibiotic-resistant carriage, but the realised public health benefits of any intervention targeting both antibiotic-resistant and antibiotic-sensitive strains will depend upon the relative health burden of susceptible versus non-susceptible *S. pneumoniae* infections; enumerating these comparative burdens is the subject of ongoing research (*55*).

Vaccination in a high-burden setting.

While our study has focused on the epidemiology of antibiotic-resistant *S. pneumoniae* in Europe, higher prevalences of carriage, disease, and resistance may be observed in lower-income settings, and it is desirable to know whether this could substantially alter predictions of vaccine impact. As an illustrative example, a 90% pneumococcal carriage

rate, with 81% of isolates resistant to penicillin, has been observed among children under five years old in western Kenya (56). This may be partly attributable to a longer average duration of carriage in this setting, as a 71-day mean duration of natural pneumococcal carriage has been measured in Kilifi, eastern Kenya (57).

To model a similar high-burden setting, we adjusted model parameters estimated from European data. Specifically, we increased the mean natural carriage duration, transmission rate, and treatment rate to match observed data, and ignored mixing with any other countries (f = 1), while keeping other parameters the same. We found that a comparatively greater vaccine efficacy is needed to reduce the prevalence of antibiotic-resistant pneumococcal carriage in a high-burden, high-resistance setting (Fig. 5). This is particularly true under the "Growth competition" model, because in this model resistant carriage only declines as total pneumococcal carriage declines, and it is particularly difficult to reduce overall carriage in a high-transmission setting. Simultaneously, vaccination may have a comparatively greater impact in high-burden settings because of a comparatively higher incidence of disease. For example, Kenya has been estimated to have an 8.8-fold higher incidence of severe pneumococcal pneumonia than the average in Europe (58).

Accounting for additional between-country variation does not substantially alter predictions.

Our focus thus far has been on the impact of the four identified mechanisms *per se* upon antibiotic resistance evolution, and accordingly we have focused on reproducing the positive association between treatment rate and resistance frequency rather than attempting to capture the additional variability in resistance frequency between countries not accounted for by the reported treatment rate alone (Fig. 2A). This additional variability may partially stem from differences in national testing and reporting practices, or between-country differences in the distribution of pneumococcal serotypes among invasive isolates (*59*). However, another possibility is that this additional variability in resistance results from systematic differences in pathogen biology or host behaviour across countries, which can be captured by our modeling framework.

To help identify which model parameters could account for this variability, we relaxed the assumption that only the treatment rate varies across countries, and performed Bayesian maximum *a posteriori* fitting, assuming one additional parameter (c, b, β , u, f, z, g, κ , a, δ , or k) is free to vary between countries while other parameters are held constant. We found that additional variation in antibiotic resistance between countries can be explained by variation in certain other parameters, depending upon which model is used (Fig. 6A, B). Importantly, among those parameters for which additional variation between countries can explain the variation in resistance (Fig. 6C), predictions for the overall impact of vaccination remain similar, with the major differences between scenarios still attributable to the underlying mechanism of antibiotic resistance evolution (Fig. 6D; Figs. S5–S16). Models that could make more accurate country-specific predictions would need to account for the effects of demographic structure, differences in carriage prevalence and disease rates between settings, and variable vaccine protection among individuals.

Discussion

Using mathematical modeling of penicillin consumption and penicillin nonsusceptibility in *S. pneumoniae* invasive isolates, we have identified four mechanisms of antibiotic resistance evolution that can recapitulate the observed relationship between penicillin consumption and penicillin non-susceptibility in *S. pneumoniae* across Europe. These mechanisms are not mutually exclusive, but the relative importance of each may have an impact upon predictions of antibiotic resistance evolution after vaccination. In particular, the "directionality" of within-host competition—that is, whether, on average, within-host competition tends to benefit antibiotic-resistant or sensitive strains strongly determines whether vaccination selects for a decrease or an increase in antibiotic resistance in the long term. This directionality may vary between pathogens, but is also sensitive to the antibiotic treatment rate, and so may also vary between settings. Although we have focused on competition between antibiotic-sensitive and resistant strains of *S. pneumoniae* only, competition between pneumococcal serotypes (24) and with other bacteria colonizing the nasopharynx will also impact antibiotic resistance evolution; determining the importance of these other sources of within-host competition is crucial.

A key finding of our models suggests that the mode of vaccine protection—whether acquisition-blocking or clearance-accelerating—has an appreciable impact upon antibiotic resistance evolution. Whole-cell and purified-protein pneumococcal vaccines may induce antibody-mediated humoral immunity, CD4+ T helper-17 cell-mediated immunity, or both, with the type of immunity mediating pneumococcal acquisition, carriage, and disease in ways that are still not fully understood (49–51). By modeling both modes of vaccine action, we have highlighted that clearance-accelerating vaccines may have increased potential for preventing the spread of antibiotic resistance, because in shortening the duration of asymptomatic carriage they limit the fitness advantage of antibiotic-resistant pathogens under selection pressure from antibiotic use.

424

425

426

427

428

429

430

431

432

433

434

435

436

437

438

439

440

441

442

443

444

445

446

447

448

449

450

451

452

453

454

455

We fitted our models to a "snapshot" of penicillin non-susceptible S. pneumoniae as observed across European countries in 2007, finding that each of the four models recapitulated the data equally well. This raises the question of what kind of data would be needed to distinguish among the four models. One possibility would be to consider trends of antibiotic resistance evolution over time. Indeed, the prevalence of penicillin non-susceptibility in S. pneumoniae remained largely stable in Europe between 2005-2017, a period which saw the incorporation of pneumococcal conjugate vaccines into the routine immunization schedules of most European countries (60). This could be viewed as favoring the "treatment diversity" and "pathogen diversity" mechanisms, which predict little change in antibiotic resistance evolution following vaccination. But because serotype replacement has largely negated any vaccine impact on the prevalence of nasopharyngeal pneumococcal carriage (10, 11), it is not clear that we would be able to detect any effects of competition-mediated antibiotic resistance evolution following a serotype-specific vaccine such as pneumococcal conjugate vaccine—particularly given the complexity of detecting vaccine-attributable changes in resistance in a population-level ecological study that would be confounded both by serotype replacement and by other changes in antibiotic resistance evolution that might be expected to occur at a national level over the course of multiple years. However, it is known that the prevalence of pneumococcal carriage declines substantially with age (42). Therefore, it might be possible to detect a signal of within-host competition between antibiotic-sensitive and resistant strains by comparing the relative prevalence

of antibiotic-resistant pneumococcal carriage in younger versus older hosts, provided that other differences could be controlled for.

456

457

458

459

460

461

462

463

464

465

466

467

468

469

470

471

472

473

474

475

476

477

478

479

480

481

482

483

484

485

486

487

488

Under the "Treatment diversity" and "Pathogen diversity" models, we have argued that universal pneumococcal vaccination will have little impact upon the longterm evolution of antibiotic resistance because it does not change the sources of diversity that modulate antibiotic resistance evolution. Nonetheless, it is possible to target vaccines such that this diversity is harnessed to manage antibiotic resistance: high-resistance serotypes could be targeted with a serotype-specific vaccine, or hightreatment subpopulations could be targeted for vaccination in order to more effectively manage resistance. Indeed, vaccination does have an additional inhibiting effect upon antibiotic resistance in our models because of the latter effect. This inhibition occurs because the vaccine has a relatively greater impact upon transmission in populations where the prevalence of pneumococcal carriage is already low, which in our models occurred in countries or subpopulations with more antibiotic consumption. Given that these populations drive antibiotic resistance more strongly, the vaccine's comparatively greater impact in these populations tends to moderately inhibit antibiotic resistance overall. We note that while previous work (38) has suggested that antibiotic resistance evolution under a "Pathogen diversity" model results in a "stepped" resistance pattern in which D-types are either fully sensitive or fully resistant at equilibrium, we find that small amounts of mixing between populations can smooth out this pattern and allow intermediate rates of resistance within subtypes (Fig. S2). Finally, while we have framed "Treatment competition" and "Growth competition" as two distinct alternatives, they can instead be viewed as endpoints on a continuum, with possible models of resistance evolution for which both c > 0 and b > 0 lying between them. The impact of vaccination on antibiotic resistance in such a model would depend upon the relative importance of treatment-mediated and growth-mediated competition.

These are some of the limitations to our study. We have focused on prevalence (the fraction of individuals who are carriers) rather than incidence (the rate of new carriage episodes) of nasopharyngeal carriage in presenting our findings. There is evidence that pneumococcal disease progression is more likely to occur shortly after nasopharyngeal acquisition (61), suggesting that incidence may be more relevant than prevalence for predicting disease outcomes. Notably, recent modeling work has suggested that clearance-accelerating vaccines could increase rates of pneumococcal

acquisition, if carriage is protective against new acquisition (due to, e.g., a founder effect) (62). More work is required to clarify the links between acquisition, carriage, and disease across competing models of pneumococcal transmission. Additionally, we have assumed that antibiotic treatment rates among pneumococcal carriers remains constant after the introduction of a vaccine, even though treatment rates dropped in many settings following the introduction of pneumococcal conjugate vaccine (5, 9). However, for a universal pneumococcal vaccine that reduces antibiotic treatment rates because it reduces carriage and thereby prevents antibiotic-treatable disease, any reduction in treatment will only occur among individuals who, because of vaccine protection, are not pneumococcal carriers, all else being equal. It might then be expected that treatment rates in pneumococcal carriers would remain equally high among those individuals for whom vaccine protection has failed—although physicians may be less inclined to prescribe antibiotics for respiratory tract infection more generally after the introduction of a new pneumococcal vaccine. Finally, we have focused on modeling data from children under 5 years old only. We would not expect incorporating age structure to lead to qualitatively different results, but age-related maturation of the immune system has been shown to be important for maintaining the circulation of pneumococcal serotypes (49) which, in turn, is a key driver of resistance evolution in the "pathogen diversity" model.

Our work helps to resolve the question: What explains the persistent coexistence between antibiotic-resistant and sensitive strains of *S. pneumoniae*? (25) by demonstrating that multiple mechanisms are capable of explaining trends of antibiotic resistance across European countries. Given that there is empirical support for withinhost competition between antibiotic-sensitive and resistant pathogen strains (63–66), heritable differences in the propensity for resistance within species (38, 67), and within-country heterogeneity in antibiotic consumption rates (68–70), all of these mechanisms likely contribute to this pattern. Our results contextualize previous mathematical studies that have variously suggested that serotype-specific vaccination may increase (24), decrease (22) or have no impact upon (18) the frequency of antibiotic resistance in *S. pneumoniae*. Whereas the potential for vaccination to promote antibiotic resistance because of competition between sensitive and resistant strains has been described previously (24), we have shown that vaccination can either promote or inhibit antibiotic resistance depending upon the directionality of within-host

competition. Whereas vaccines targeting highly-resistant serotypes can decrease antibiotic resistance (22), we have shown that a serotype-independent vaccine promoting accelerated natural clearance can decrease resistance across all circulating subtypes. And where single-population models have found no long-term impact of vaccination on antibiotic resistance frequency (18), we have shown that in multi-population models, vaccination can inhibit resistance if it has a larger impact in subpopulations that consume more antibiotics. The direction and magnitude of this effect would depend upon variation in vaccine uptake, vaccine efficacy, and pathogen transmission among subpopulations, and we have not systematically explored this variation here.

A highly efficacious serotype-independent pneumococcal vaccine can indeed reduce the overall burden of antibiotic-resistant pneumococcal infections. However, the long-term effect upon antibiotic resistance of a vaccine with intermediate efficacy is less certain, as vaccine impact depends crucially upon the mechanisms that drive antibiotic resistance evolution. Thus, empirical investigation of pathogen competitive dynamics—and the impact of setting-specific factors on these dynamics—is needed to make accurate predictions of vaccine impact on antibiotic-resistant infections.

Materials and Methods

541 Study design.

This study comprised four parts: (1) A literature search used to identify plausible mechanisms through which coexistence can be maintained between antibiotic-sensitive and resistant pneumococcal strains across a range of antibiotic treatment rates; (2) a mathematical modeling study embedding these mechanisms of antibiotic resistance evolution in four models of pneumococcal transmission; (3) a Bayesian statistical analysis to fit these models to empirically observed frequencies of penicillin non-susceptibility and community penicillin consumption across 27 European countries for the year 2007; (4) a vaccine impact analysis using these fitted models to forecast the impact of a universal pneumococcal vaccine. We used data from 2007 because changes in pneumococcal resistance reporting standards for some countries after this year would hamper the between-country comparability of data (71). Our objectives were to identify the mechanisms potentially responsible for maintaining coexistence between antibiotic-resistant and sensitive pneumococci in Europe, and to determine whether the

impact of vaccination on the evolution of antibiotic resistance depends upon which mechanism is assumed to operate.

557

555

556

- 558 Literature search for mechanisms driving antibiotic resistance.
- We searched PubMed using the terms: (AMR OR ABR OR ((antimicrobial OR antibiotic)
- AND resist*)) AND ((model OR modelling OR modeling) AND (dynamic* OR transmi* OR
- mathematical)) AND (coexist* OR intermediate). This yielded 93 papers (Table S1). We
- included all papers containing a dynamic host-to-host pathogen transmission model
- analysing both antibiotic-sensitive and resistant strains with stable coexistence as an
- outcome of the model. From the 11 studies meeting these criteria, we identified nine
- unique mechanisms, two of which correspond to alternative parameterisations of a
- within-host competition model. We ruled out four mechanisms because of
- implausibility or because previous work showed that the mechanism does not bring
- about substantial coexistence, leaving four mechanisms (Table 1).

569

- 570 Model framework.
- We analysed the evolution of antibiotic resistance by tracking the transmission of
- resistant and sensitive bacterial strains among hosts in a set of *M* countries indexed by
- 573 $m \in \{1, 2, ..., M\}$ using systems of ordinary differential equations.

574

- In a simple model, hosts can either be non-carriers (X), carriers of the sensitive strain
- 576 (S), or carriers of the resistant strain (R). Omitting country-specific subscripts *m* for
- 577 concision, model dynamics within a country are captured by

578

579
$$dS/dt = \lambda_S X - (u + \tau)S$$

580
$$dR/dt = (1 - c)\lambda_R X - uR$$

$$581 X = 1 - S - R, (1)$$

- where λ_S is the force of infection of the sensitive strain, λ_R is the force of infection of the
- resistant strain, *c* is the transmission cost of resistance, *u* is the rate of natural
- clearance, and τ is the treatment rate. In this model, in a given country, the total
- carriage of the sensitive strain is *S* and the total carriage of the resistant strain is *R*.

Force of infection terms are defined below; a summary of all model parameters can be found in Table S2.

The "Treatment diversity" model extends the simple model (eq. 1) by structuring each country into multiple subpopulations that exhibit different rates of antibiotic treatment and make contact with each other at unequal rates (25, 34, 35, 72). In each country, we model N equally-sized representative subpopulations indexed by $i \in \{1,2,...,N\}$, where we assume N = 10. Dynamics within a country are

596
$$dS_{i}/dt = \lambda_{S,i}X - (u + \tau_{i})S$$
597
$$dR_{i}/dt = (1 - c)\lambda_{R,i}X - uR$$
598
$$X_{i} = 1 - S_{i} - R_{i}$$
(2)

where we assume that treatment rates of subpopulations within a country approximately follow a gamma distribution with shape parameter κ and mean treatment rate τ . Accordingly, the rate of antibiotic consumption in subpopulation i is $O_{\Gamma}(\frac{i}{L}|\kappa)$

 $\tau_i = \int_{Q_{\Gamma}\left(\frac{i-1}{N}|\kappa\right)}^{Q_{\Gamma}\left(\frac{i}{N}|\kappa\right)} t \, P_{\Gamma}(t|\kappa) \, dt, \text{ where } Q_{\Gamma}(q|\kappa) \text{ is the quantile } q \text{ of the gamma distribution}$

with shape κ and $P_{\Gamma}(t|\kappa)$ is the probability density at t of the same gamma distribution.

At the scale of individuals, antibiotic consumption is highly variable, with some people

taking no antibiotics in a given year and others taking many courses of antibiotics (73);

at regional scales, antibiotic consumption shows less extreme variability (74) and

approaches a normal distribution. We use a gamma distribution to model variation in

treatment rates among subpopulations because it can capture patterns at either of these

scales, or scales in between.

The "Pathogen diversity" model extends the simple model (eq. 1) by structuring the pathogen population into D different "D-types" (we assume D = 25), each with a different natural clearance rate, where each type is kept circulating by diversifying selection acting on D-type (38). Dynamics within a country are

617
$$dS_d/dt = q_d \lambda_{S,d} X - (u_d + \tau) S_d$$
618
$$dR_d/dt = q_d (1 - c) \lambda_{R,d} X - u_d R_d$$

619
$$X = 1 - \Sigma_d (S_d + R_d)$$
 (3)

620

- where q_d is the strength of diversifying selection for D-type $d \in \{1,2,\dots,D\}$ and u_d is
- the clearance rate for D-type d. We follow Lehtinen et al. (38) in defining $q_d =$

623
$$\left(1 - \frac{S_d + R_d}{\sum_{j=1}^D (S_j + R_j)} + \frac{1}{D}\right)^a$$
 and $u_d = u\left(1 + \delta\left(2\frac{d-1}{D-1} - 1\right)\right)$, where a is the power of

- diversifying selection and δ is the range of clearance rates. In a given country, the total
- carriage of the type-d sensitive strain is S_d and the total carriage of the type-d resistant
- 626 strain is R_d .

627

- 628 Finally, the within-host competition models (26) allow hosts to carry a mix of both
- strains. Hosts can carry the sensitive strain with a small complement of the resistant
- strain (S_R) or the resistant strain with a small complement of the sensitive strain (R_S).
- 631 Dynamics within a country are

632

633
$$dS/dt = \lambda_{S}X - (u + \tau)S - k(1 - c)\lambda_{R}S + b_{0}S_{R}$$

634
$$dS_R/dt = k(1-c)\lambda_R S - (u+\tau)S_R + bR_S - b_0 S_R$$

635
$$dR_S/dt = k\lambda_S R - (u + \tau)R_S - bR_S$$

636
$$dR/dt = (1-c)\lambda_R X - uR - k\lambda_S R + \tau (S_R + R_S)$$

637
$$X = 1 - S - R - S_R - R_S,$$
 (4)

638

- where *k* is the rate of co-colonisation relative to primary colonisation, *b* is the within-
- host growth benefit of sensitivity (i.e. the rate of the $R_S \rightarrow S_R$ transition), and b_0 is the
- rate of the $S_R \rightarrow S$ transition. We follow Davies *et al.* (26) in setting $b_0 = 4b$. In a given
- country, the total carriage of the sensitive strain is $S + S_R$ and the total carriage of the
- resistant strain is $R + R_s$. "Treatment competition" assumes the cost of resistance is
- incurred by reduced transmission potential (b = 0 and c > 0), while "Growth
- competition" assumes that the cost of resistance is incurred through decreased within-
- 646 host growth (b > 0 and c = 0).

- In equations 1, 3 and 4, the force of infection of a particular strain A in country m is $\lambda_A =$
- 649 $\beta (f A_{tot|m} + (1-f) \sum_{\ell=1}^{M} h_{\ell} A_{tot|\ell})$, where β is the transmission rate, f is the between-
- 650 country assortativity, h_{ℓ} is the relative population size of country m (such that $\sum_{\ell} h_{\ell} =$

651 1), and $A_{\text{tot}|\ell}$ is the total carriage of strain A in country ℓ . The probability with which individuals contact an individual from another country, 1 - f, captures those contacts 652 653 made with individuals from another country in either one's home country or a foreign country. In equation 2, the force of infection of a particular strain A in subpopulation i of 654 country m is $\lambda_{A,i} = \beta \left(f \left(g A_{\text{tot}|m,i} + (1-g) \sum_{j=1}^{N} \frac{1}{N} A_{\text{tot}|m,j} \right) + (1-g) \sum_{j=1}^{N} \frac{1}{N} A_{\text{tot}|m,j} \right) + (1-g) \sum_{j=1}^{N} \frac{1}{N} A_{\text{tot}|m,j} + (1-g)$ 655 $f)\sum_{\ell=1}^{M}\sum_{j=1}^{N}\frac{h_{\ell}}{N}A_{\text{tot}|\ell,j}$), where g is the within-country assortativity and $A_{\text{tot}|\ell,j}$ is the 656 657 total carriage of strain A in subpopulation j of country ℓ . 658 659 Data and model fitting. 660 We extracted community penicillin consumption and penicillin non-susceptibility in S. pneumoniae invasive isolates from databases made available by the ECDC (13, 28). We 661 662 assumed that community penicillin consumption drives penicillin resistance, that 663 antibiotic consumption is independent of whether an individual is colonised by 664 pneumococcus, and that resistance among invasive bacterial isolates is representative of resistance among circulating strains more broadly. Countries report community 665 666 penicillin consumption in defined daily doses (DDD) per thousand individuals per day. To transform this bulk consumption rate into the rate at which individuals undertake a 667 668 course of antibiotic therapy, we analysed prescribing data from eight European countries, estimating that, on average, 5 DDD in the population at large correspond to 669 670 one treatment course for a child under 5 years of age. This conversion rate varies 671 between countries (Table S3), but since the data are incomplete (8 of 27 countries) we 672 have not explicitly accounted for this variability in our main model fitting results. 673 674 Our model framework tracks carriage of S. pneumoniae among children less than 5 675 years old, the age group driving both transmission and disease. In European countries, 676 we assumed that the prevalence of pneumococcal carriage in under-5s is 50% (11, 42) 677 and the average duration of carriage is 47 days (47, 48). We calculated the average 678 incidence of *S. pneumoniae*-caused severe pneumonia requiring hospitalisation as 610 679 per million children under 5 per year (58) across the European countries in our data

set. See Tables S4, S5, and S6 for details of calculations relating to pneumococcal

carriage duration and disease incidence.

680

681

We used Bayesian inference via differential evolution Markov chain Monte Carlo (75) to

identify model parameters that are consistent with empirical data while accounting for

uncertainty in those estimates. Country m has antibiotic treatment rate τ_m and reports

- 686 r_m of n_m isolates are resistant. Over all M countries, these data are denoted $\tau =$
- 687 $(\tau_1, \tau_2, ..., \tau_M), r = (r_1, r_2, ..., r_M), \text{ and } n = (n_1, n_2, ..., n_M), \text{ respectively.}$ The probability of
- 688 a given set of model parameters θ is then
- 689 $P(\theta|\tau,r,n) \propto P(\tau,r,n|\theta)P(\theta),$

690

684

where $P(\theta)$ is the prior probability of parameters θ and

692
$$P(\tau, r, n|\theta) = C(Y = Y(\tau|\theta)) \prod_{m=1}^{M} R(r = r_m, n = n_m, \rho = \rho(\tau_m|\theta))^{N_m/\bar{N}}$$

693

- is the likelihood of data τ , r, n given model parameters θ . Above, $Y(\theta)$ is the average
- model-predicted prevalence of carriage across all countries and $\rho(\tau_m|\theta)$ is the model-
- 696 predicted resistance prevalence for country m. C(Y) is the credibility of prevalence of
- carriage *Y* and $R(r,n,\rho)$ is the credibility of *r* out of *n* isolates being resistant when the
- model-predicted resistance prevalence is ρ . For C(Y), we use a normal distribution with
- 699 mean 0.5 and standard deviation 0.002. For $R(r,n,\rho)$, we use $R(r,n,\rho) =$
- 700 $\int_0^1 T(x|\mu=\rho,\sigma=\sigma(\theta))\binom{n}{r}x^r(1-x)^{n-r}\,dx$, a binomial distribution where the
- 701 probability of success is modelled as a [0,1]-truncated normal distribution centred on ρ
- and with standard deviation σ . The parameter σ captures the unexplained between-
- country variation in resistance frequency. Here, $T(x|\mu,\sigma) = \frac{\varphi(x|\mu,\sigma)}{\left(\Phi(1|\mu,\sigma) \Phi(0|\mu,\sigma)\right)}$, where
- 704 $\varphi(\mu, \sigma) = \frac{1}{\sqrt{2\pi\sigma^2}} exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ is the untruncated normal PDF and $\Phi(\mu, \sigma) = \frac{1}{2}(1 + \frac{1}{2})$
- 705 $erf\left(\frac{x-\mu}{\sigma\sqrt{2}}\right)$) is the untruncated normal cumulative distribution function. Finally, N_m is the
- 706 population size of country m and \overline{N} is the average population size across all countries;
- 707 the exponent N_m/\bar{N} allows us to weight the importance of each country by its
- 708 population size, which allows a closer fit with the overall resistance prevalence across
- 709 all countries.

- As prior distributions for parameter inference, we adopted $c \sim \text{Beta}(\alpha = 1.5, \beta = 8.5)$,
- 712 $b \sim \text{Gamma}(\kappa = 2, \theta = 0.5), \beta \sim \text{Gamma}(\kappa = 5, \theta = 0.35), g \sim \text{Beta}(\alpha = 10, \beta = 1.5),$

- 713 $\kappa \sim \text{Gamma}(\kappa = 4, \theta = 2), \alpha \sim \text{Gamma}(\kappa = 2, \theta = 5), \delta \sim \text{Beta}(\alpha = 20, \beta = 25), \text{ and}$
- 714 $k \sim \text{Normal}(\mu = 1, \sigma = 0.5)$. Priors for *c*, *b*, and β were chosen to be vague since these
- parameters are heavily constrained by the data we fitted our models to. Priors for g, κ ,
- 716 a, δ , and k were chosen to keep parameters within biologically plausible ranges. Table
- 717 S7 provides more detail on the choice of priors, and Fig. S4 shows which parameters are
- 718 most strongly constrained by these prior beliefs.

719

- We set the unexplained between-country variation in resistance prevalence σ to 0.06
- across all models based on a preliminary round of model fitting with σ as a free
- parameter. We set the between-country assortativity f to 0.985 (i.e., 1.5% of contacts
- occur with individuals from a different country) based on rates of travel for EU
- residents. Specifically, using Eurostat database tour_dem_tnw (76) we estimated that
- the average EU resident spent 1.5% of their nights abroad in 2007; this overestimates
- mixing because children under 5 travel less than the average person, but
- underestimates mixing because it does not account for contacts made with visitors to an
- individual's country of residence and because children may contract pneumococcal
- 729 carriage from adults who travel, and so we kept the value of 1.5%. See Table S8 for
- 730 MCMC diagnostics.

731

- To match model predictions to a high-burden setting, we increased the duration of
- carriage to 71.4 days; increased the transmission rate by a factor of 3.49 (Treatment
- diversity), 3.62 (Pathogen diversity), 3.61 (Treatment competition), or 3.20 (Growth
- competition), so that carriage prevalence reached 90.0%; and increased the antibiotic
- consumption rate to 1.670, 1.458, 1.138, or 5.887 courses per person per year,
- respectively, so that resistance prevalence reached 81.4%.

738

- 739 *Vaccine impact analysis*
- 740 Interventions have the following impact on model parameters: for the acquisition-
- blocking vaccine, the transmission rate becomes $\beta' = (1 \epsilon_a) \beta$; for the clearance-
- 742 accelerating vaccine, the clearance rate becomes $u' = u/(1-\varepsilon_c)$; and under antibiotic
- stewardship, the average treatment rate in each country *m* becomes $\tau_m' = \tau_m (1 \varepsilon_s)$.

744

745 *Capturing additional between-country variation in antibiotic resistance frequency.*

We began by finding the maximum a posteriori model fits according to the likelihood and prior distributions for each of the four models of antibiotic resistance evolution. This identified the following parameter values for each model. "Treatment diversity": β = 1.41, c = 0.124, g = 0.976, and κ = 2.22. "Pathogen diversity": β = 1.33, c = 0.191, a = 10.8, and δ = 0.608. "Treatment competition": β = 1.42, c = 0.191, and k = 1.64. "Growth competition": $\beta = 1.39$, b = 0.195, and k = 1.61. Then, we performed maximum a *posteriori* model fits for each potentially-varying parameter under each model, allowing the varying parameter to take on a different value for each country and fixing other parameters at their maximum *a posteriori* values as determined in the previous step, or at specific assumed values for u = 0.65, f = 0.985, and z = 5. For the second step, we used a modified likelihood function

758
$$P(\tau, r, n | \theta) = C(Y = Y(\tau | \theta)) \prod_{m=1}^{M} \phi \left(\mu = \frac{r_m + 1}{n_m + 2}, \sigma = 0.001 \middle| x = \rho(\tau_m | \theta) \right)^{N_m / \bar{N}},$$

where $\phi(\mu, \sigma|x)$ is the normal probability density function. This modified likelihood function ensures that the model-predicted resistance frequency for each country is matched as closely as possible to the maximum-likelihood resistance prevalence $\frac{r_m+1}{n_m+2}$ (i.e., assuming a uniform prior on resistance frequency) for each country m, so that model fits are comparable across different varying parameters. We used the Nelder-Mead algorithm to maximize the posterior probability in both steps.

Figs. S5–S8 show maximum *a posteriori* fits when allowing an additional parameter to vary freely between countries, along with the parameter values identified by model fitting. Figs. S9–S12 show the impact of vaccination, focusing on those parameters for which model fitting was able to capture the observed variability in antibiotic resistance frequency between countries (*i.e.*, those parameters plotted to the left of the dashed line in Fig. 6B of the main text). Figs. S13–S16 show the impact of vaccination for the remaining parameters.

Statistics used in this study.

We used Bayesian inference, via Markov chain Monte Carlo techniques, in this study. We summarized the resulting posterior distributions using means and highest density intervals (HDIs), which differ from equal-tailed credible intervals in that they estimate the most compact region of support that contains a given proportion (e.g., 95%) of the posterior density.

- **Supplementary Materials**
- **Fig. S1-S16**
- **Table S1-S8.**

References and Notes

- 787 1. J. O'Neill, "Vaccines and alternative approaches: reducing our dependence on
- 788 antimicrobials" (2016), (available at http://amr-
- review.org/sites/default/files/Vaccines and alternatives_v4_LR.pdf).
- 790 2. M. Lipsitch, R. Siber, How Can Vaccines Contribute to Solving the Antimicrobial
- 791 Resistance Problem ? **7**, 1–8 (2016).
- 792 3. K. E. Atkins, M. Lipsitch, Can antibiotic resistance be reduced by vaccinating
- against respiratory disease? *Lancet Respir. Med.* **6**, 820–821 (2018).
- 794 4. J. P. Sevilla, D. E. Bloom, D. Cadarette, M. Jit, M. Lipsitch, Toward economic
- 795 evaluation of the value of vaccines and other health technologies in addressing
- 796 AMR. Proc. Natl. Acad. Sci. **115**, 12911–12919 (2018).
- 797 5. K. P. Klugman, S. Black, Impact of existing vaccines in reducing antibiotic
- resistance: Primary and secondary effects. *Proc. Natl. Acad. Sci.* **115**, 12896–
- 799 12901 (2018).
- 800 6. M. H. Kyaw, R. Lynfield, W. Schaffner, A. S. Craig, J. Hadler, A. Reingold, A. R.
- Thomas, L. H. Harrison, N. M. Bennett, M. M. Farley, R. R. Facklam, J. H. Jorgensen,
- J. Besser, E. R. Zell, A. Schuchat, C. G. Whitney, Effect of Introduction of the
- Pneumococcal Conjugate Vaccine on Drug-Resistant Streptococcus pneumoniae.
- 804 N. Engl. J. Med. **354**, 1455–1463 (2006).
- 7. D. Thorrington, N. Andrews, J. Stowe, E. Miller, A. J. van Hoek, Elucidating the
- impact of the pneumococcal conjugate vaccine programme on pneumonia, sepsis
- and otitis media hospital admissions in England using a composite control. *BMC*
- 808 *Med.* **16**, 1–14 (2018).
- 809 8. C. Chen, F. Cervero Liceras, S. Flasche, S. Sidharta, J. Yoong, N. Sundaram, M. Jit,
- 810 Effect and cost-effectiveness of pneumococcal conjugate vaccination: a global
- modelling analysis. *Lancet Glob. Heal.* **7**, e58–e67 (2019).
- 812 9. K. J. Wilby, D. Werry, A review of the effect of immunization programs on
- antimicrobial utilization. *Vaccine*. **30**, 6509–6514 (2012).
- 814 10. W. P. Hanage, J. A. Finkelstein, S. S. Huang, S. I. Pelton, A. E. Stevenson, K.
- Kleinman, V. L. Hinrichsen, C. Fraser, Evidence that pneumococcal serotype
- replacement in Massachusetts following conjugate vaccination is now complete.
- 817 Epidemics. 2, 80–84 (2010).

- 818 11. S. Flasche, A. J. Van Hoek, E. Sheasby, P. Waight, N. Andrews, C. Sheppard, R.
- George, E. Miller, Effect of pneumococcal conjugate vaccination on serotype-
- specific carriage and invasive disease in England: a cross-sectional study. *PLoS*
- 821 *Med.* **8**, e1001017 (2011).
- 822 12. J. A. Lewnard, W. P. Hanage, Making sense of differences in pneumococcal
- serotype replacement. *Lancet Infect. Dis.* **3099** (2019), doi:10.1016/s1473-
- 824 3099(18)30660-1.
- 825 13. European Centre for Disease Prevention and Control, Antimicrobial consumption
- rates by country (2018), (available at
- http://ecdc.europa.eu/en/healthtopics/antimicrobial_resistance/esac-net-
- database/Pages/Antimicrobial-consumption-rates-by-country.aspx).
- 829 14. World Health Organization, WHO vaccine pipeline tracker (2019), (available at
- https://www.who.int/immunization/research/vaccine_pipeline_tracker_spreads
- 831 heet/en/).
- 832 15. G. L. Masala, M. Lipsitch, C. Bottomley, S. Flasche, Exploring the role of
- competition induced by non-vaccine serotypes for herd protection following
- pneumococcal vaccination. J. R. Soc. Interface. 14 (2017),
- 835 doi:10.1098/rsif.2017.0620.
- 836 16. K. E. Atkins, E. I. Lafferty, S. R. Deeny, N. G. Davies, J. V. Robotham, M. Jit, Use of
- mathematical modelling to assess the impact of vaccines on antibiotic resistance.
- 838 *Lancet Infect. Dis.* **18**, e204–e213 (2018).
- 839 17. K. E. Atkins, S. Flasche, Vaccination to reduce antimicrobial resistance. *Lancet*
- 840 *Glob. Heal.* **6**, e252 (2018).
- 18. L. Temime, D. Guillemot, P. Y. Boëlle, Short- and long-term effects of
- pneumococcal conjugate vaccination of children on penicillin resistance.
- 843 *Antimicrob. Agents Chemother.* **48**, 2206–2213 (2004).
- 844 19. L. Temime, P. Y. Boëlle, A. J. Valleron, D. Guillemot, Penicillin-resistant
- pneumococcal meningitis: High antibiotic exposure impedes new vaccine
- protection. *Epidemiol. Infect.* **133**, 493–501 (2005).
- 847 20. L. Opatowski, L. Temime, E. Varon, R. Leclerc, H. Drugeon, P.-Y. Boëlle, D.
- Guillemot, Antibiotic Innovation May Contribute to Slowing the Dissemination of
- Multiresistant Streptococcus pneumoniae: The Example of Ketolides. *PLoS One.* **3**,
- 850 e2089 (2008).

- 21. T. Van Effelterre, M. R. Moore, F. Fierens, C. G. Whitney, L. White, S. I. Pelton, W. P.
- Hausdorff, A dynamic model of pneumococcal infection in the United States:
- Implications for prevention through vaccination. *Vaccine*. **28**, 3650–3660 (2010).
- 854 22. M. D. De Cellès, M. Pons-Salort, E. Varon, M. A. Vibet, C. Ligier, V. Letort, L.
- Opatowski, D. Guillemot, Interaction of vaccination and reduction of antibiotic use
- drives unexpected increase of pneumococcal meningitis. *Sci. Rep.* **5**, 1–11 (2015).
- 857 23. P. K. Mitchell, M. Lipsitch, W. P. Hanage, Carriage burden, multiple colonization
- and antibiotic pressure promote emergence of resistant vaccine escape
- pneumococci. *Philos. Trans. R. Soc. B Biol. Sci.* **370**, 3–9 (2015).
- 860 24. U. Obolski, J. Lourenço, C. Thompson, R. Thompson, A. Gori, S. Gupta, Vaccination
- can drive an increase in frequencies of antibiotic resistance among nonvaccine
- serotypes of Streptococcus pneumoniae. *Proc. Natl. Acad. Sci.* **115**, 3102–3107
- 863 (2018).
- 864 25. C. Colijn, T. Cohen, C. Fraser, W. Hanage, E. Goldstein, N. Givon-Lavi, R. Dagan, M.
- Lipsitch, What is the mechanism for persistent coexistence of drug-susceptible
- and drug-resistant strains of *Streptococcus pneumoniae? J. R. Soc. Interface.* **7**,
- 867 905–919 (2010).
- 868 26. N. G. Davies, S. Flasche, M. Jit, K. E. Atkins, Within-host dynamics shape antibiotic
- resistance in commensal bacteria. *Nat. Ecol. Evol.* (2019), doi:10.1038/s41559-
- 870 018-0786-x.
- 871 27. H. Goossens, M. Ferech, R. Vander Stichele, M. Elseviers, Outpatient antibiotic use
- in Europe and association with resistance: A cross-national database study.
- 873 *Lancet.* **365**, 579–587 (2005).
- 874 28. European Centre for Disease Prevention and Control, Data from the ECDC
- Surveillance Atlas Antimicrobial resistance (2016), (available at
- https://ecdc.europa.eu/en/antimicrobial-resistance/surveillance-and-disease-
- 877 data/data-ecdc).
- 878 29. M. Lipsitch, C. Colijn, T. Cohen, W. P. Hanage, C. Fraser, No coexistence for free:
- Neutral null models for multistrain pathogens. *Epidemics*. **1**, 2–13 (2009).
- 880 30. P. Rodrigues, M. G. M. Gomes, C. Rebelo, Drug resistance in tuberculosis-a
- reinfection model. *Theor. Popul. Biol.* **71**, 196–212 (2007).
- 882 31. O. Patterson-Lomba, B. M. Althouse, G. M. Goerg, L. Hébert-Dufresne, Optimizing
- Treatment Regimes to Hinder Antiviral Resistance in Influenza across Time

- 884 Scales. *PLoS One*. **8**, 1–11 (2013).
- 885 32. I. M. Hastings, Complex dynamics and stability of resistance to antimalarial drugs.
- 886 *Parasitology.* **132**, 615–624 (2006).
- 887 33. R. Sergeev, C. Colijn, T. Cohen, Models to understand the population-level impact
- of mixed strain M. tuberculosis infections. *J. Theor. Biol.* **280**, 88–100 (2011).
- 889 34. F. Blanquart, S. Lehtinen, M. Lipsitch, C. Fraser, The evolution of antibiotic
- resistance in a structured host population. *J. R. Soc. Interface.* **15** (2018),
- 891 doi:10.1098/rsif.2018.0040.
- 892 35. M. S. Krieger, A. L. Hill, Long-term coexistence and regional heterogeneity of
- antibiotic-resistant infections reproduced by a simple spatial model. *bioRxiv*. **14**,
- 894 469171 (2018).
- 895 36. R. Kouyos, E. Klein, B. Grenfell, Hospital-Community Interactions Foster
- 896 Coexistence between Methicillin-Resistant Strains of Staphylococcus aureus. *PLoS*
- 897 *Pathog.* **9** (2013), doi:10.1371/journal.ppat.1003134.
- 898 37. M. F. Boni, M. W. Feldman, Evolution of Antibiotic Resistance By Human and
- Bacterial Niche Construction. *Evolution (N. Y).* **59**, 477 (2006).
- 900 38. S. Lehtinen, F. Blanquart, N. J. Croucher, P. Turner, M. Lipsitch, C. Fraser, Evolution
- of antibiotic resistance is linked to any genetic mechanism affecting bacterial
- 902 duration of carriage. *Proc. Natl. Acad. Sci.* **114**, 1075–1080 (2017).
- 903 39. D. J. Austin, K. G. Kristinsson, R. M. Anderson, The relationship between the
- volume of antimicrobial consumption in human communities and the frequency
- 905 of resistance. *Proc. Natl. Acad. Sci.* **96**, 1152–1156 (1999).
- 906 40. A. B. Beams, D. J. A. Toth, K. Khader, F. R. Adler, Harnessing intra-host strain
- competition to limit antibiotic resistance: mathematical model results. *Bull. Math.*
- 908 *Biol.* **78**, 1828–1846 (2016).
- 909 41. K. Græsbøll, S. S. Nielsen, N. Toft, L. E. Christiansen, How fitness reduced,
- antimicrobial resistant bacteria survive and spread: A multiple pig multiple
- 911 bacterial strain model. *PLoS One.* **9** (2014), doi:10.1371/journal.pone.0100458.
- 912 42. D. Bogaert, A. Van Belkum, M. Sluijter, A. Luijendijk, R. De Groot, H. C. Rümke, H. A.
- Verbrugh, P. W. M. Hermans, Colonisation by *Streptococcus pneumoniae* and
- 914 *Staphylococcus aureus* in healthy children. *Lancet.* **363**, 1871–1872 (2004).
- 915 43. D. M. Weinberger, V. E. Pitzer, G. Regev-Yochay, N. Givon-Lavi, R. Dagan,
- Association between the Decline in Pneumococcal Disease in Unimmunized

- 917 Adults and Vaccine-Derived Protection Against Colonization in Toddlers and
- 918 Preschool-Aged Children. *Am. J. Epidemiol.* **188**, 160–168 (2019).
- 919 44. D. I. Andersson, The biological cost of mutational antibiotic resistance: any
- 920 practical conclusions? *Curr. Opin. Microbiol.* **9** (2006), pp. 461–465.
- 921 45. D. I. Andersson, D. Hughes, Antibiotic resistance and its cost: Is it possible to
- 922 reverse resistance? *Nat. Rev. Microbiol.* **8**, 260–271 (2010).
- 923 46. C. Tedijanto, S. Olesen, Y. Grad, M. Lipsitch, Estimating the proportion of
- bystander selection for antibiotic resistance among potentially pathogenic
- 925 bacterial flora. *Proc Natl Acad Sci USA*. **115**, E11988–E11995 (2018).
- 926 47. L. Högberg, P. Geli, H. Ringberg, E. Melander, M. Lipsitch, K. Ekdahl, Age- and
- 927 serogroup-related differences in observed durations of nasopharyngeal carriage
- of penicillin-resistant pneumococci. J. Clin. Microbiol. 45, 948–952 (2007).
- 929 48. A. Melegaro, N. J. Gay, G. F. Medley, Estimating the transmission parameters of
- pneumococcal carriage in households. *Epidemiol. Infect.* **132**, 433–441 (2004).
- 931 49. S. Cobey, M. Lipsitch, Niche and neutral effects of acquired immunity permit
- 932 coexistence of pneumococcal serotypes. *Science* (80-.). **335**, 1376–1380 (2012).
- 933 50. R. Malley, P. W. Anderson, Serotype-independent pneumococcal experimental
- vaccines that induce cellular as well as humoral immunity. *Proc. Natl. Acad. Sci. U.*
- 935 *S. A.* **109**, 3623–3627 (2012).
- 936 51. S. P. Jochems, J. N. Weiser, R. Malley, D. M. Ferreira, The immunological
- mechanisms that control pneumococcal carriage. *PLoS Pathog.* **13**, 1–14 (2017).
- 938 52. UK Department of Health and Social Care, "Tackling antimicrobial resistance 2019
- to 2024: the UK's 5-year national action plan" (2019), (available at
- 940 https://www.gov.uk/government/publications/uk-5-year-action-plan-for-
- 941 antimicrobial-resistance-2019-to-2024).
- 942 53. B. S. Buckley, N. Henschke, H. Bergman, B. Skidmore, E. J. Klemm, G. Villanueva, C.
- Garritty, M. Paul, Impact of vaccination on antibiotic usage: a systematic review
- and meta-analysis. Clin. Microbiol. Infect. In press (2019),
- 945 doi:10.1016/j.cmi.2019.06.030.
- 946 54. A. Von Gottberg, L. De Gouveia, S. Tempia, V. Quan, S. Meiring, C. Von Mollendorf,
- 947 S. A. Madhi, E. R. Zell, M. Stat, J. R. Verani, K. L. O'Brien, C. G. Whitney, K. P.
- Klugman, C. Cohen, Effects of vaccination on invasive pneumococcal disease in
- 949 South Africa. N. Engl. J. Med. **371**, 1889–1899 (2014).

- 950 55. A. Cassini, L. D. Högberg, D. Plachouras, A. Quattrocchi, A. Hoxha, G. S. Simonsen,
- 951 M. Colomb-Cotinat, M. E. Kretzschmar, B. Devleesschauwer, M. Cecchini, D. A.
- Ouakrim, T. C. Oliveira, M. J. Struelens, C. Suetens, D. L. Monnet, R. Strauss, K.
- 953 Mertens, T. Struyf, B. Catry, K. Latour, I. N. Ivanov, E. G. Dobreva, A. Tambic
- Andraševic, S. Soprek, A. Budimir, N. Paphitou, H. Žemlicková, S. Schytte Olsen, U.
- Wolff Sönksen, P. Märtin, M. Ivanova, O. Lyytikäinen, J. Jalava, B. Coignard, T.
- 956 Eckmanns, M. Abu Sin, S. Haller, G. L. Daikos, A. Gikas, S. Tsiodras, F. Kontopidou,
- 957 Á. Tóth, Á. Hajdu, Ó. Guólaugsson, K. G. Kristinsson, S. Murchan, K. Burns, P.
- 958 Pezzotti, C. Gagliotti, U. Dumpis, A. Liuimiene, M. Perrin, M. A. Borg, S. C. de Greeff,
- J. C. Monen, M. B. Koek, P. Elstrøm, D. Zabicka, A. Deptula, W. Hryniewicz, M.
- Caniça, P. J. Nogueira, P. A. Fernandes, V. Manageiro, G. A. Popescu, R. I. Serban, E.
- 961 Schréterová, S. Litvová, M. Štefkovicová, J. Kolman, I. Klavs, A. Korošec, B. Aracil, A.
- Asensio, M. Pérez-Vázquez, H. Billström, S. Larsson, J. S. Reilly, A. Johnson, S.
- Hopkins, Attributable deaths and disability-adjusted life-years caused by
- infections with antibiotic-resistant bacteria in the EU and the European Economic
- Area in 2015: a population-level modelling analysis. *Lancet Infect. Dis.* **19**, 56–66
- 966 (2019).
- 967 56. M. Kobayashi, L. M. Conklin, G. Bigogo, G. Jagero, L. Hampton, K. E. Fleming-Dutra,
- 968 M. Junghae, M. da G. Carvalho, F. Pimenta, B. Beall, T. Taylor, K. F. Laserson, J.
- Vulule, C. Van Beneden, L. Kim, D. R. Feikin, C. G. Whitney, R. F. Breiman,
- Pneumococcal carriage and antibiotic susceptibility patterns from two cross-
- 971 sectional colonization surveys among children aged <5 years prior to the
- introduction of 10-valent pneumococcal conjugate vaccine Kenya, 2009-2010.
- 973 *BMC Infect. Dis.* **17**, 1–12 (2017).
- 974 57. M. Lipsitch, O. Abdullahi, A. D'Amour, W. Xie, D. M. Weinberger, E. Tchetgen
- Tchetgen, J. A. G. Scott, Estimating rates of carriage acquisition and clearance and
- competitive ability for pneumococcal serotypes in Kenya with a Markov
- 977 transition model. *Epidemiology*. **23**, 510–519 (2012).
- 978 58. I. Rudan, K. L. O'Brien, H. Nair, L. Liu, E. Theodoratou, S. Qazi, I. Luksic, C. L. F.
- 979 Walker, R. E. Black, H. Campbell, Child Health Epidemiology Reference Group,
- 980 Epidemiology and etiology of childhood pneumonia in 2010: estimates of
- incidence, severe morbidity, mortality, underlying risk factors and causative
- pathogens for 192 countries. *J. Glob. Health.* **3**, S114-010401 (2013).

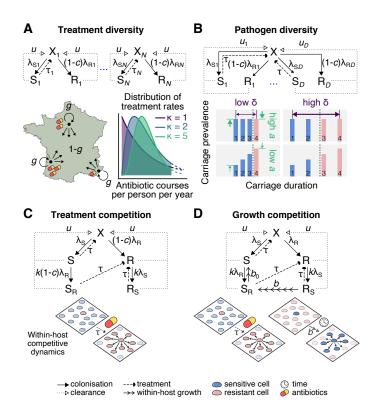
- 983 59. A. N. Torné, J. G. Dias, C. Quinten, F. Hruba, M. C. Busana, P. L. Lopalco, A. J. A.
- Gauci, L. Pastore-Celentano, M. Sabbe, J. Verhaegen, M. Koliou, D. Pieridou-
- 985 Bagkatzouni, P. Křižovà, J. Kozakova, J. Motlova, P. Valentiner-Branth, L.
- Lambertsen, T. Georgakopoulou, H. Humphreys, T. Melillo, P. Caruana, M. Knol, H.
- de Merkel, K. Elberse, D. Frimann, A. Skoczynska, W. Hryniewicz, A. Kuch, I.
- Paradowska-Stankiewicz, M. Pana, M. Vitek, V. Učakar, B. H. Normark, T. Lepp, M.
- 989 Slack, P. A. Waight, European enhanced surveillance of invasive pneumococcal
- disease in 2010: Data from 26 European countries in the post-heptavalent
- 991 conjugate vaccine era. *Vaccine*. **32**, 3644–3650 (2014).
- 992 60. M. Tin Tin Htar, D. Christopoulou, H. J. Schmitt, Pneumococcal serotype evolution
- 993 in Western Europe. *BMC Infect. Dis.* **15**, 1–10 (2015).
- 994 61. B. Simell, K. Auranen, H. Käyhty, D. Goldblatt, R. Dagan, K. L. O'Brien, The
- 995 fundamental link between pneumococcal carriage and disease. Expert Rev.
- 996 *Vaccines.* **11**, 841–855 (2012).
- 997 62. S. Flasche, A. Guilder, Using a mathematical model to assess the potential effects
- of a new vaccine approach that targets enhanced clearance of pneumococcal
- 999 carriage. (2018).
- 1000 63. M. C. Negri, M. Lipsitch, J. Blázquez, B. R. Levin, F. Baquero, Concentration-
- dependent selection of small phenotypic differences in TEM beta-lactamase-
- mediated antibiotic resistance. *Antimicrob. Agents Chemother.* **44**, 2485–91
- 1003 (2000).
- 1004 64. A. R. Wargo, S. Huijben, J. C. de Roode, J. Shepherd, A. F. Read, Competitive release
- and facilitation of drug-resistant parasites after therapeutic chemotherapy in a
- 1006 rodent malaria model. *Proc. Natl. Acad. Sci.* **104**, 19914–19919 (2007).
- 1007 65. N. Wale, D. G. Sim, M. J. Jones, R. Salathe, T. Day, A. F. Read, Resource limitation
- prevents the emergence of drug resistance by intensifying within-host
- 1009 competition. *Proc. Natl. Acad. Sci.*, 201715874 (2017).
- 1010 66. J. A. Lewnard, P. A. Tähtinen, M. K. Laine, L. Lindholm, J. Jalava, P. Huovinen, M.
- Lipsitch, A. Ruohola, Impact of antimicrobial treatment for acute otitis media on
- carriage dynamics of penicillin-susceptible and penicillin-non-susceptible
- 1013 Streptococcus pneumoniae. J. Infect. Dis., jiy343 (2018).
- 1014 67. S. Lehtinen, F. Blanquart, M. Lipsitch, C. Fraser, On the evolutionary ecology of
- multidrug resistance in bacteria. *PLoS Pathog.* **15**, 1–22 (2019).

- 1016 68. M. Filippini, G. Masiero, K. Moschetti, Socioeconomic determinants of regional
- differences in outpatient antibiotic consumption: Evidence from Switzerland.
- 1018 *Health Policy (New. York).* **78**, 77–92 (2006).
- 1019 69. D. Koller, F. Hoffmann, W. Maier, K. Tholen, R. Windt, G. Glaeske, Variation in
- antibiotic prescriptions: Is area deprivation an explanation? Analysis of 1.2
- million children in Germany. *Infection*. **41**, 121–127 (2013).
- 1022 70. M. Di Martino, A. Lallo, U. Kirchmayer, M. Davoli, D. Fusco, Prevalence of antibiotic
- prescription in pediatric outpatients in Italy: The role of local health districts and
- primary care physicians in determining variation. A multilevel design for
- healthcare decision support. *BMC Public Health*. **17**, 1–8 (2017).
- 1026 71. M. C. Goossens, B. Catry, J. Verhaegen, Antimicrobial resistance to benzylpenicillin
- in invasive pneumococcal disease in Belgium, 2003-2010: The effect of altering
- 1028 clinical breakpoints. *Epidemiol. Infect.* **141**, 490–495 (2013).
- 1029 72. S. Cobey, E. B. Baskerville, C. Colijn, W. Hanage, C. Fraser, M. Lipsitch, Host
- population structure and treatment frequency maintain balancing selection on
- drug resistance. J. R. Soc. Interface. **14**, 20170295 (2017).
- 1032 73. A. Pottegård, A. Broe, R. Aabenhus, L. Bjerrum, J. Hallas, P. Damkier, Use of
- antibiotics in children: A danish nationwide drug utilization study. *J. Pediatr.*
- 1034 *Infect. Dis.* **34**, e16–e22 (2015).
- 1035 74. W. V. Kern, K. De With, K. Nink, M. Steib-Bauert, H. Schröder, Regional variation in
- outpatient antibiotic prescribing in Germany. *Infection.* **34**, 269–273 (2006).
- 1037 75. C. Ter Braak, A Markov Chain Monte Carlo version of the genetic algorithm
- Differential Evolution: Easy Bayesian computing for real parameter spaces. *Stat.*
- 1039 *Comput.* **16**, 239–249 (2006).
- 1040 76. Eurostat (2019), (available at https://ec.europa.eu/eurostat/home?).
- 1041 77. T. Smieszek, K. B. Pouwels, F. C. K. Dolk, D. R. M. Smith, S. Hopkins, M. Sharland, A.
- D. Hay, M. V Moore, J. V Robotham, Potential for reducing inappropriate antibiotic
- prescribing in English primary care. *J. Antimicrob. Chemother.* **73**, ii36–ii43
- 1044 (2018).

1046 Acknowledgements 1047 1048 Funding: N.G.D., M.J. and K.E.A. were funded by the National Institute for Health 1049 Research Health Protection Research Unit in Immunisation at the London School of 1050 Hygiene and Tropical Medicine in partnership with Public Health England. The views 1051 expressed are those of the authors and not necessarily those of the NHS, National 1052 Institute for Health Research, Department of Health or Public Health England. S.F. was 1053 supported by a Sir Henry Dale Fellowship jointly funded by the Wellcome Trust and 1054 Royal Society (grant number 208812/Z/17/Z). 1055 1056 *Author contributions:* All authors designed the study. N.G.D. performed the analyses 1057 with input from K.E.A., M.J., and S.F. The paper was written by N.G.D. and K.E.A. with 1058 input from M.J. and S.F. 1059 1060 *Competing interests:* The authors declare no competing interests. 1061 1062 Data and Materials Availability: All data and code used in this study have been 1063 deposited to Zenodo with DOI 10.5281/zenodo.5116454.

1064 Figures

1065



10661067

1068

1069

1070

1071

1072

1073

1074

1075

1076

1077

1078

1079

1080

1081

1082

Fig. 1. Four models of antibiotic resistance evolution. This figure illustrates the four mechanisms that this study identifies as potential explanations for the association between penicillin consumption and penicillin non-susceptibility in *Streptococcus* pneumoniae across 27 European countries. Each mechanism is captured by a different mathematical model, the structure and key features of which are illustrated here. In the diagrams above, X hosts are uncolonised, S hosts are colonised with the antibioticsensitive strain and R hosts are colonised with the antibiotic-resistant strain. Force-ofinfection terms λ_A are equal to the person-to-person contact rate β times the probability that a contacted individual carries strain *A*; *c* is the transmission cost of resistance; *u* is the natural clearance rate; and τ is the rate of antibiotic treatment. (A) "Treatment diversity" model: Each country is split into subpopulations varying in treatment rate τ_i , with treatment rates drawn from a gamma distribution with shape κ. Within a country, individuals assort with their own subpopulation with probability g; this assortative mixing among treatment-varying subpopulations allows coexistence between antibiotic sensitive and resistant strains. **(B)** "Pathogen diversity" model: The pathogen comes in multiple subtypes maintained by diversifying selection, each with its own natural

carriage duration u_d^{-1} . Diversifying selection is stronger (*i.e.*, more equalizing) as a increases, while carriage durations span a greater range as δ increases. Only those subtypes whose carriage duration exceeds a critical threshold (dashed line) are selected for antibiotic resistance, so that overall, both antibiotic sensitive and resistant strains can circulate. **(C)** "Treatment competition" model: Singly-colonised hosts can acquire a small amount of another strain at relative rate k (host states S_R and R_S). Dually-colonized hosts only transmit the dominant strain, so there is within-host competition between co-colonising strains. Population-level coexistence is maintained by antibiotic treatment-mediated within-host competition. **(D)** "Growth competition" model: As in panel C, but the transmission cost of resistance is removed and sensitive strains now outgrow resistant strains within co-colonised hosts at rate b. Coexistence is maintained by both treatment-mediated and growth-mediated within-host competition. Panels A-D illustrate alternative model dynamics for a single country; our full model framework tracks dynamics for 27 European countries simultaneously, which themselves mix with assortativity f.

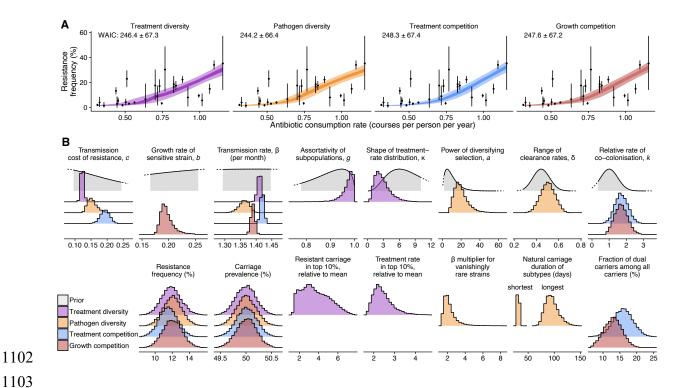


Fig 2. Four models reproduce patterns of antibiotic resistance in *S. pneumoniae* **in Europe. (A)** Model fits with associated Widely Applicable Information Criteria (WAIC, ± standard error) for the four models presented in Figure 1: Treatment diversity, Pathogen diversity, Treatment competition, Growth competition. Points and vertical lines show the mean and 95% highest density intervals (HDIs) for the reported proportion of invasive *S. pneumoniae* isolates that are resistant to penicillin plotted against the penicillin consumption rate in children under five years of age for 27 countries (source: European Centre for Disease Prevention and Control). Ribbons show the 50% and 95% HDIs for antibiotic resistance prevalence from each fitted model. **(B)** The top row shows estimated posterior distributions for the free parameters in each model; the bottom row shows model outputs associated with these parameters to aid interpretation.

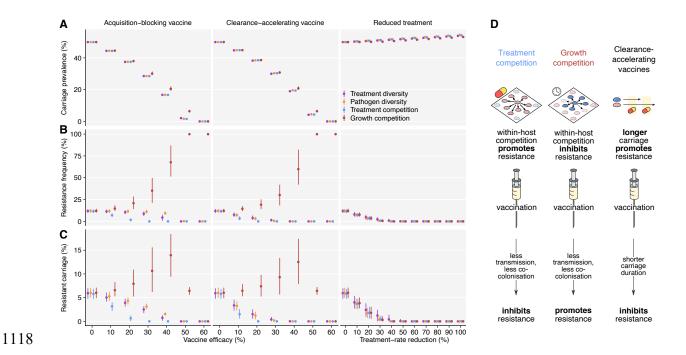


Fig. 3. Impact of vaccination and antibiotic treatment on model outcomes. Shown is the impact of vaccination with an acquisition-blocking vaccine or a clearance-accelerating vaccine, or reduced antibiotic treatment on **(A)** pneumococcal carriage prevalence, **(B)** antibiotic resistance frequency, and **(C)** antibiotic-resistant pneumococcal carriage (mean and 95% HDI) in the four models. **(D)** Illustration of the strongest forces selecting for greater or lesser antibiotic resistance across the four models.

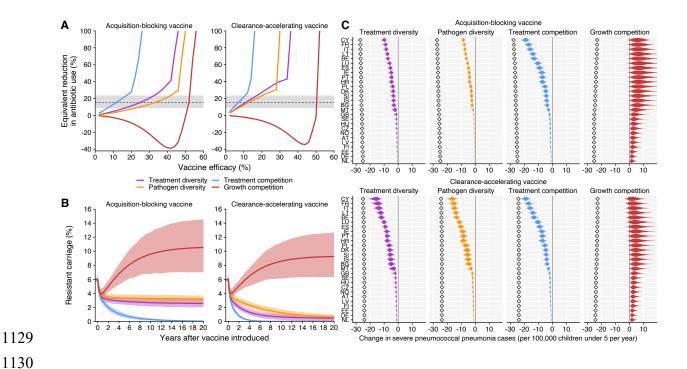


Fig. 4. Policy considerations of the four models. (A) Shown is the median equivalent reduction in prescribing antibiotics across the four models of antibiotic resistance evolution, in terms of vaccine efficacy at reducing the prevalence of resistant pneumococcal carriage. This demonstrates the vaccine efficacy required to achieve a similar decrease in antibiotic-resistant pneumococcal carriage to a given reduction in antibiotic prescription rates. The impact on overall pneumococcal carriage is not considered here. The shaded bar shows an 8.8–23.1% reduction in prescriptions, an estimate of the percentage of prescriptions in the UK which are clinically unnecessary (77). The dashed line shows a 15% reduction in prescriptions, which has recently been announced as a target by the UK government (52). **(B)** The full impact of vaccination on antibiotic resistance evolution, illustrated here with 30% vaccine efficacy, can take 5-20 years to play out (mean and 95% HDI). **(C)** Per-country impact of vaccination at 30% efficacy is shown. European countries reporting to ECDC are ordered from lowest (NL) to highest (CY) reported rate of penicillin consumption. Diamonds show the estimated change in all pneumococcal pneumonia cases; filled distributions show the change in antibiotic-resistant pneumonia cases.

1132

1133

1134

1135

1136

1137

1138

1139

1140

1141

1142

1143

1144

1145

1146

1147

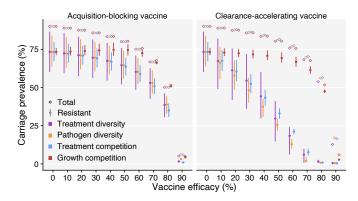


Fig. 5. Vaccine impact in a high-burden setting. Our study focuses on patterns of antibiotic consumption and resistance observed in European countries, and shows that the alternative mechanisms that could explain these patterns each yield differing predictions for how vaccination might impact upon selection for antibiotic resistance. However, these predictions depend upon the epidemiological situation in a given country. Indeed, adjusting the four fitted models to be consistent with a higher-burden setting, as is often observed in lower-income countries, yields different predictions for the impact of acquisition-blocking and clearance-accelerating vaccines on antibiotic resistance evolution (shown: mean and 95% HDI).

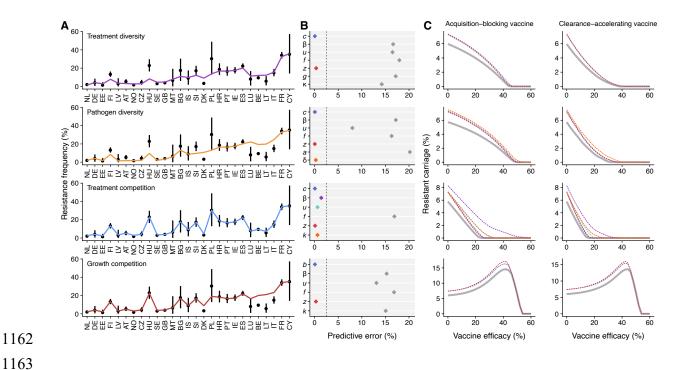


Fig 6. Explaining additional between-country variation in antibiotic resistance frequency. Allowing model parameters to vary across countries captures additional between-country variation in antibiotic resistance frequency not captured by variation in the antibiotic treatment rate. For example, (A) allowing the transmission rate β to vary across countries can explain the variation in some but not all models (points and vertical lines show mean credible antibiotic resistance frequency and 95% HDI for each country). (B) Depending upon which parameter is allowed to vary, the four models differ in how well they explain all additional between-country variation, with a clear separation (dashed line) between flexible and inflexible models. (C) Model-specific predictions for the impact of vaccination among those parameters that do fully capture the observed variation remain similar. Solid grey lines show "base" model; dashed lines correspond with colors in panel B.

Table 1. Mechanisms for maintaining coexistence of antibiotic-resistant and

sensitive S. pneumoniae

Mechanism		Mode of action	Plausible mechanism for coexistence in <i>S. pneumoniae</i> ?	Consistent with empirical patterns? (Fig. 2)
	Treatment diversity	Assortatively-mixing subpopulations differ in treatment rates (25, 34–37)	✓ Yes	✓ Yes
COMPETITION DIVERSITY	Pathogen diversity	Subtypes maintained by diversifying selection differ in propensity for resistance (38)	Yes	Yes
	Treated class	Individuals currently in treatment maintain resistant strains (25, 34, 39, 40)	No: Only supports a small amount of coexistence (25)	N/A
	Within-host niches	Sensitive and resistant strains exploit separate niches within the host (30, 41)	No: Resistant and sensitive strains are known to occupy the same niches (29)	N/A
	Mutation pressure	Mutation-selection balance maintains intermediate resistance frequency (30, 31, 37)	No: De novo acquisition of resistance in <i>S. pneumoniae</i> is not frequent enough (25)	N/A
	Prescription feedback	Doctors reduce prescribing of a drug as resistance to it increases (37, 39)	No: Does not explain how coexistence is maintained over a range of treatment rates	N/A
	Within-host competition: Treatment competition	Within-host competition creates frequency-dependent selection for resistance (25, 26, 32, 33, 40)	✓ Yes	✓ Yes
	Within-host competition: Growth competition	Within-host competition creates frequency-dependent selection for resistance (25, 26, 32, 33, 40)	Yes	Yes
9	Superinfection	Superinfection creates frequency-dependent selection for resistance (30)	No: Requires resistant strain to transmit better than sensitive strain in absence of antibiotics	N/A

1181	Supplementary Materials for
1182	
1183	Modeling the effect of vaccination
1184	on selection for antibiotic resistance
1185	in S. pneumoniae
1186	
1187	Nicholas G. Davies, Stefan Flasche, Mark Jit, Katherine E. Atkins

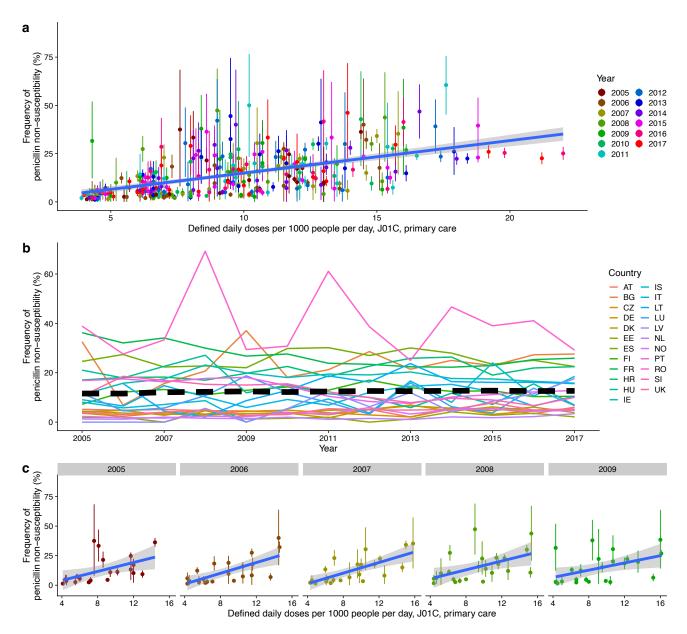


Fig. S1. Patterns of penicillin non-susceptibility across European countries, 2005–2017. (a) The frequency of penicillin non-susceptibility in pneumococcal isolates (mean and 95% HDI) increases with the primary care consumption of penicillins, ATC class J01C (least-squares linear regression $\beta=0.0168$, F(1,344)=148.5, $P<2.2\times10^{-16}$). Data from Belgium after 2007 are excluded because of changes to the definition of penicillin non-susceptibility after this year. (b) The frequency of penicillin non-susceptibility has fluctuated in individual countries between 2005 and 2017, but the European population-weighted average (thick dashed line) has remained stable at roughly 12%. (c) We fit our models to the prevalence of penicillin non-susceptibility in 2007. Despite the introduction of pneumococcal conjugate vaccines into many

European national immunisation programmes starting in 2006, pneumococcal resistance appears to have been relatively stable over the time period 2005–2009: while mean penicillin non-susceptibility across European countries increased by 0.5% per year over this time period, and the slope of penicillin non-susceptibility on primary-care penicillin consumption decreased by 0.1%/DDD per year, neither of these changes are significant (least-squares linear regression: F(1,3) = 0.64, P = 0.48 and F(1,3) = 1.48, P = 0.31, respectively).

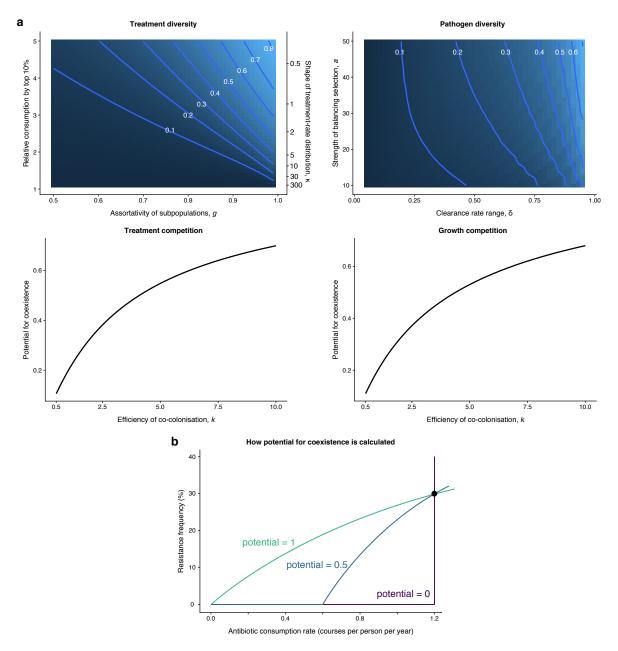


Fig. S2. Impact of key parameters upon the potential for coexistence in each model. (a) Potential for coexistence for each model, depending upon key parameters. In the top two panels, darker colours represent lower potential for coexistence while lighter colours represent higher potential for coexistence. (b) Schematic showing how to calculate the "potential for coexistence", an ad-hoc measurement of how much coexistence is exhibited by a given model under a given parameterisation. To find it, we set $\beta = 1.4$ months⁻¹, u = 0.7 months⁻¹, and set g, κ , δ , a, and k according to the values shown in the figure (panel a). We then numerically identify the value of c (or b for the "growth competition" model) which results in the equilibrium resistance frequency passing through exactly 30% for a single country in which the antibiotic consumption

rate is equal to τ = 1.2 courses per person per year (black dot; these values are chosen to approximately match observations for *S. pneumoniae* in European countries). The potential for coexistence is the probability that the equilibrium resistance frequency is above 0 for a random treatment rate between τ = 0 and τ = 1.2 (in other words, it is the proportion of the curve that "lifts off" from the x-axis; see figure). By this definition, a model showing no coexistence has potential 0, while a model showing the maximum amount of coexistence has potential 1.

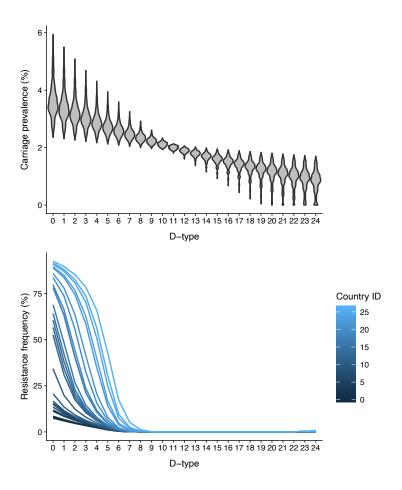


Fig. S3. Carriage and resistance of D-types in the "Pathogen diversity" model. This verifies that the D-types with the highest prevalence of carriage (averaged over all countries, above) also exhibit the highest resistance frequency (separated by country, below), and shows that at equilibrium, D-types can exhibit intermediate frequencies of resistance.

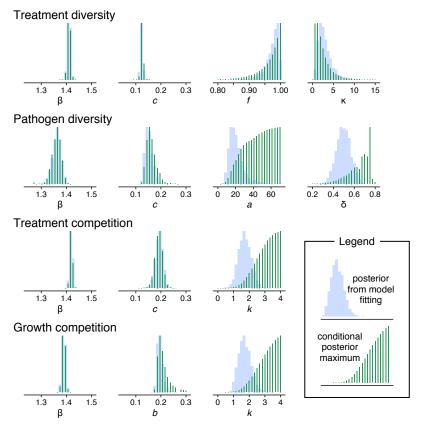


Fig. S4. Comparison of inferred model posteriors and conditional posterior maxima for each parameter. The conditional posterior maximum (green bars) is obtained by fixing the parameter of interest at a specific value, then allowing the other parameters to assume their maximum *a posteriori* values through numerical optimization of the model fit. This is repeated for multiple values of the parameter of interest. The position on the x-axis of the thin green bars shows these fixed values for the parameter of interest (chosen to "sweep" across the parameter range), while the height of the thin green bars is relative to the maximum posterior probability conditional on that fixed value. When the conditional posterior maximum (green bars) does not align with the posteriors from model fitting (blue bars, same as Fig. 2b, main text), this indicates that the prior distribution is strongly influencing the posterior distribution for a given parameter. This analysis shows that values inferred for a and b under the "Pathogen diversity" model, and for b under the "Treatment competition" and "Growth competition" models, are strongly constrained by prior beliefs about plausible ranges for those parameters, while other parameters are less constrained.

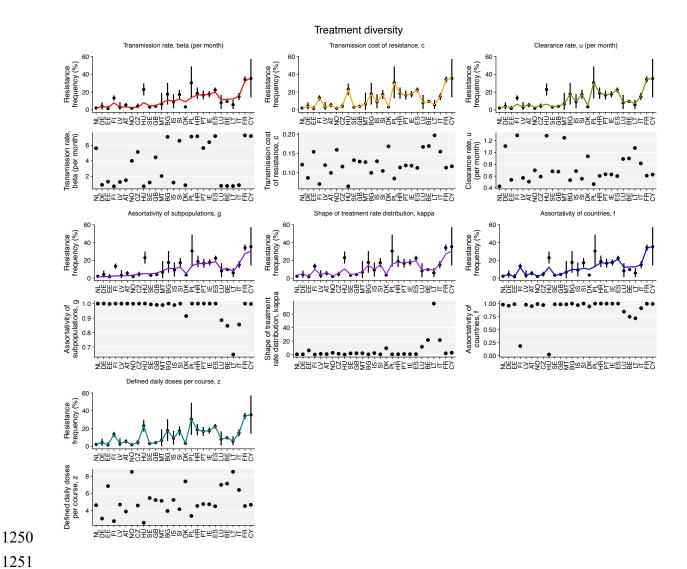


Fig. S5. Varying-parameter fits for the "Treatment diversity" model. Maximum a posteriori fits for the "Treatment diversity" model allowing one parameter to vary between countries. Parameters c and z can capture the additional variation in resistance frequency between countries.

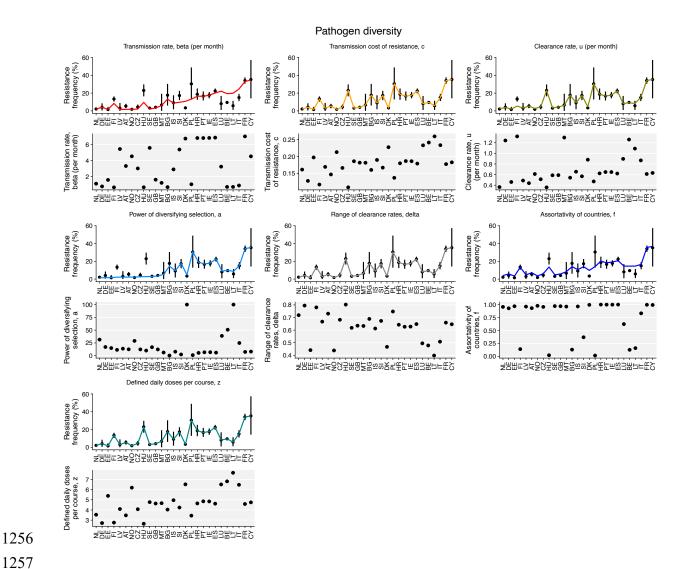


Fig. S6. Varying-parameter fits for the "Pathogen diversity" model. Maximum a *posteriori* fits for the "Pathogen diversity" model allowing one parameter to vary between countries. Parameters c, δ , and z can capture the additional variation in resistance frequency between countries.

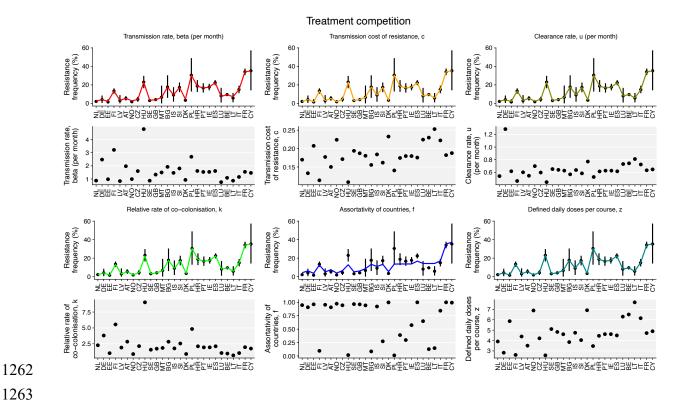


Fig. S7. Varying-parameter fits for the "Treatment competition" model. Maximum *a posteriori* fits for the "Treatment competition" model allowing one parameter to vary between countries. Parameters β , c, u, k, and z can capture the additional variation in resistance frequency between countries.

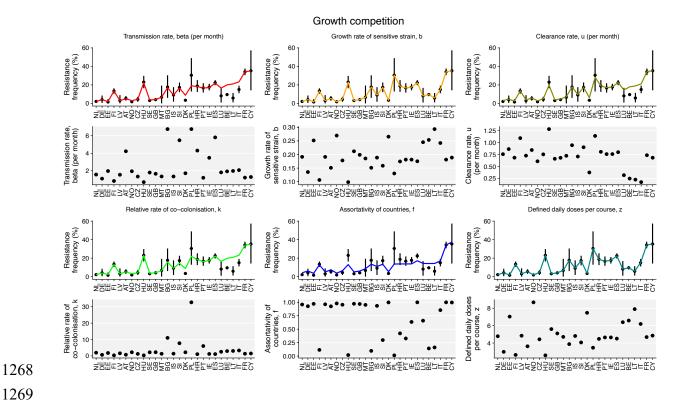


Fig. S8. Varying-parameter fits for the "Growth competition" model. Maximum a *posteriori* fits for the "Growth competition" model allowing one parameter to vary between countries. Parameters b and z can capture the additional variation in resistance frequency between countries.

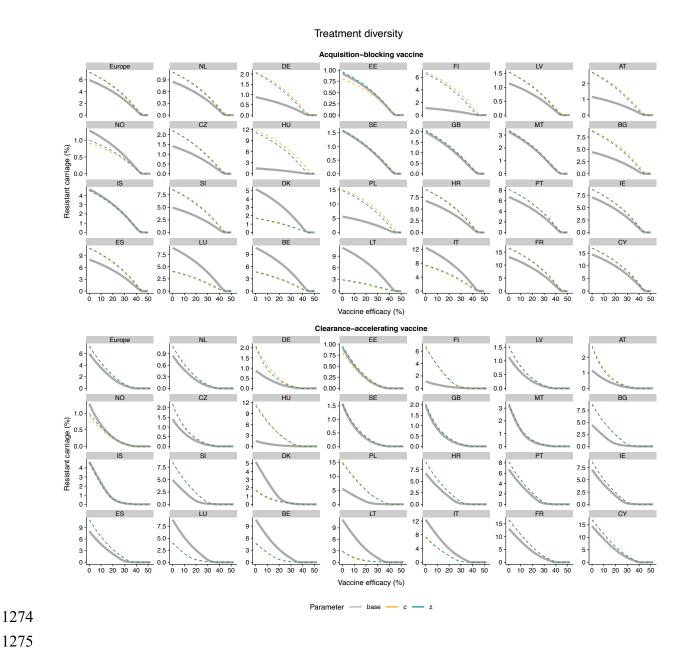


Fig. S9. Vaccine impact for the "Treatment diversity" model, varying parameters *c* and *z*. Impact of vaccination under the "Treatment diversity" model, for those parameters able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

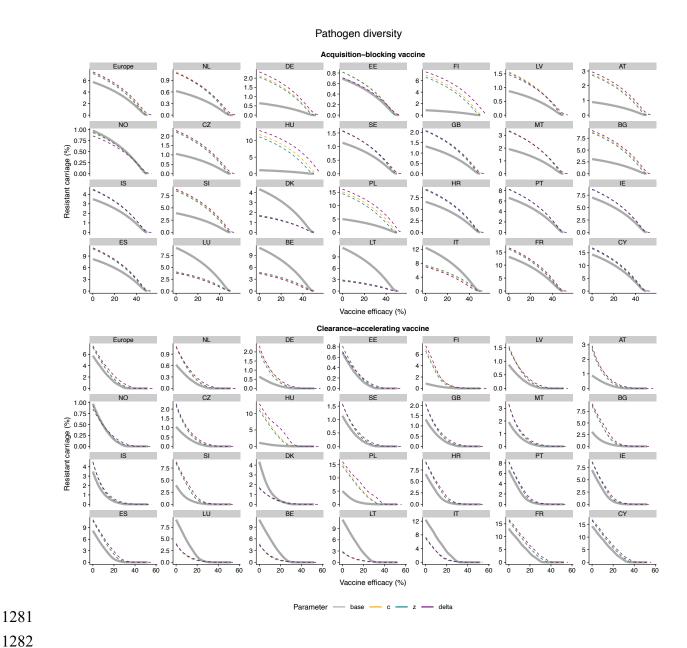


Fig. S10. Vaccine impact for the "Pathogen diversity" model, varying parameters *c*, **δ**, and *z*. Impact of vaccination under the "Pathogen diversity" model, for those parameters able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

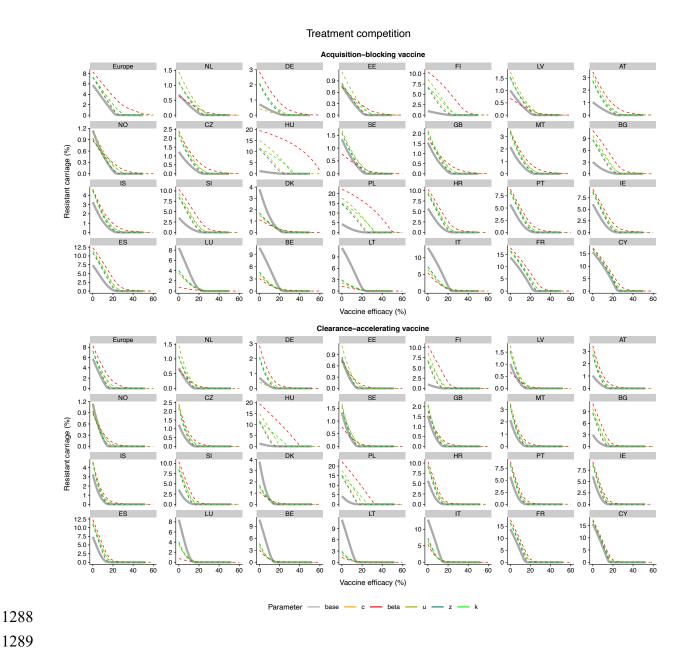


Fig. S11. Vaccine impact for the "Treatment competition" model, varying parameters β , c, u, k, and z. Impact of vaccination under the "Treatment competition" model, for those parameters able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

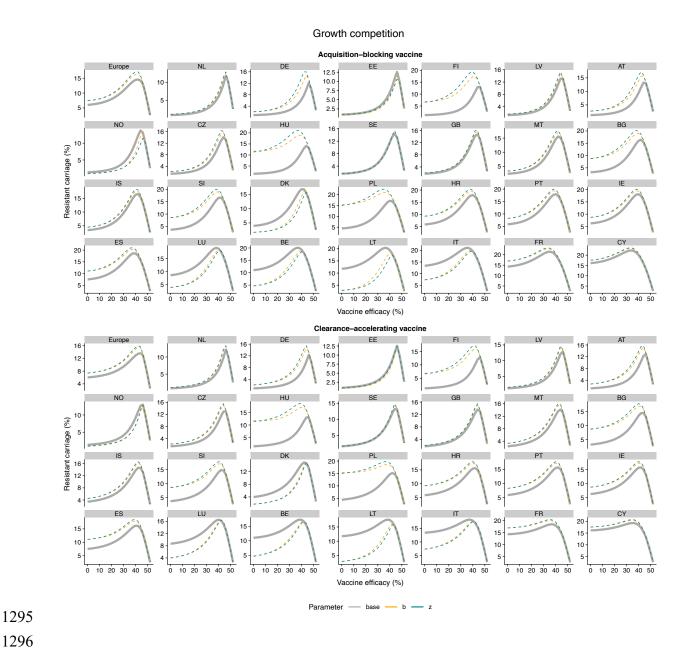


Fig. S12. Vaccine impact for the "Growth competition" model, varying parameters **b** and **z**. Impact of vaccination under the "Growth competition" model, for those parameters able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

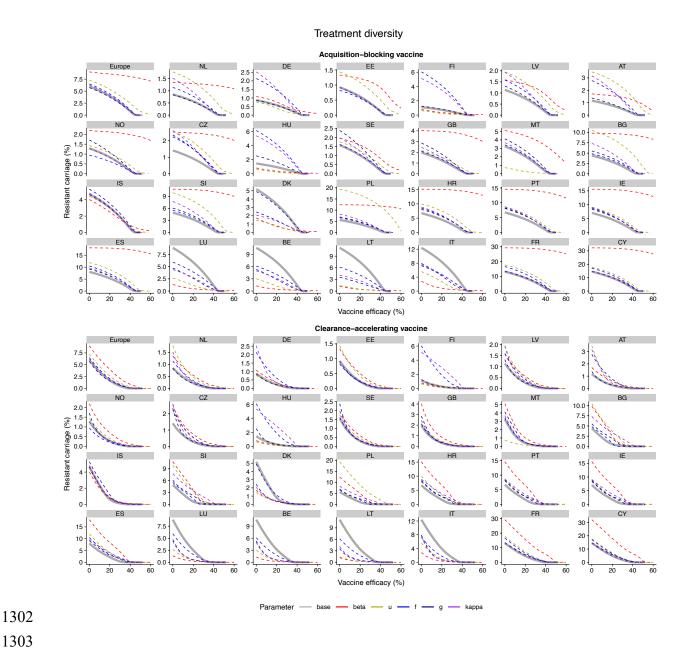


Fig. S13. Vaccine impact for the "Treatment diversity" model, varying other parameters. Impact of vaccination under the "Treatment diversity" model, for those parameters *not* able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

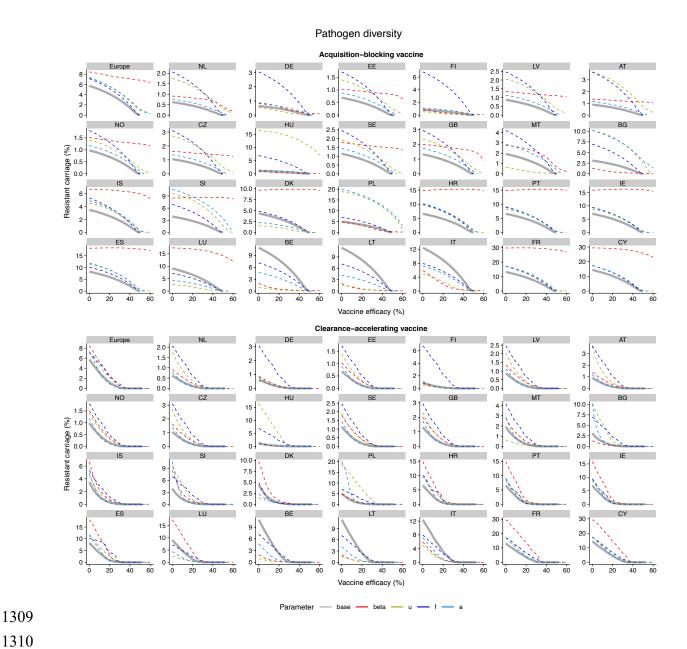


Fig. S14. Vaccine impact for the "Pathogen diversity" model, varying other parameters. Impact of vaccination under the "Pathogen diversity" model, for those parameters *not* able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

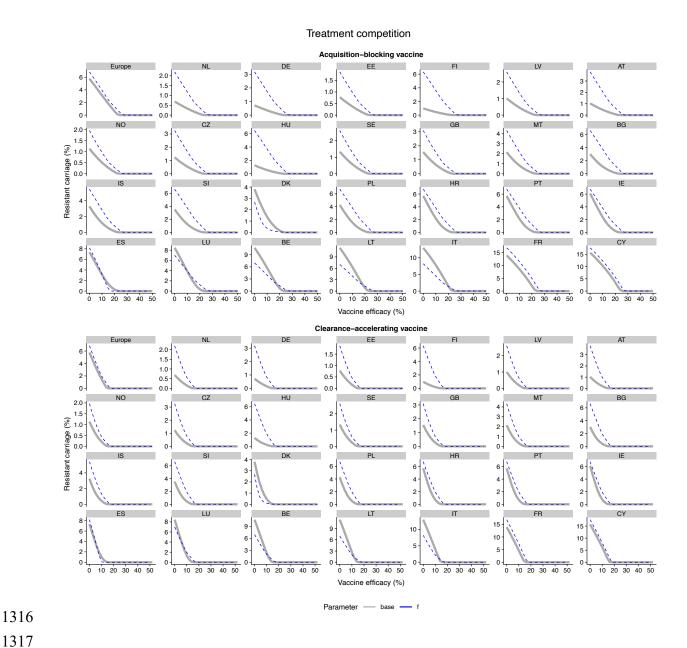


Fig. S15. Vaccine impact for the "Treatment competition" model, varying other parameters. Impact of vaccination under the "Treatment competition" model, for those parameters *not* able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

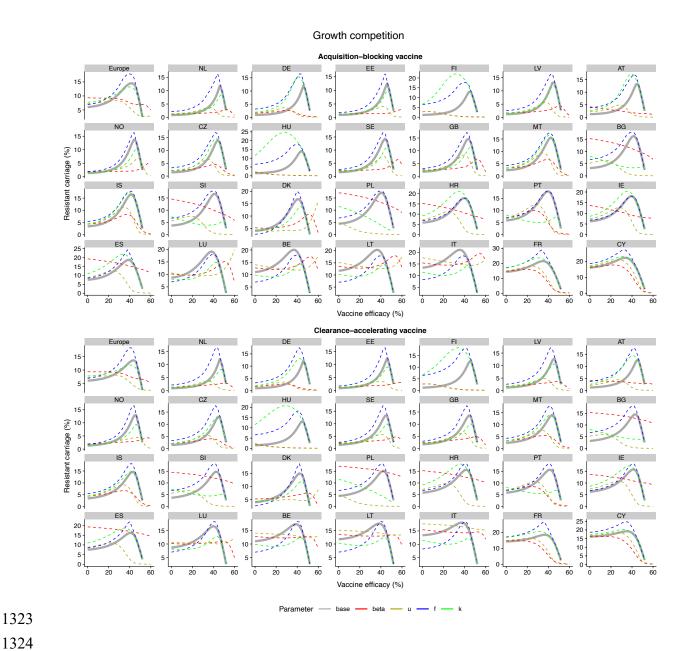


Fig. S16. Vaccine impact for the "Growth competition" model, varying other parameters. Impact of vaccination under the "Growth competition" model, for those parameters *not* able to capture the between-country variation in resistance frequency. The base model fit (thick grey solid line) is compared with the model fits in which parameters vary between countries (thin dashed lines).

1331	Tables S1-S8
1332	
1333	These tables can be found in an Excel spreadsheet accompanying the article.
1334	
1335	Table S1. Literature review — Details of the literature review used to identify
1336	mechanisms for maintaining coexistence between sensitive and resistant bacterial
1337	strains.
1338	
1339	Table S2. Summary of model parameters — Table describing model parameters and
1340	assumed values or prior distributions for model fitting.
1341	
1342	Table S3. Penicillin consumption — Calculation of the mean number of defined daily
1343	doses of penicillin corresponding to a single treatment course for children under 5
1344	years old in European countries.
1345	
1346	Table S4. Carriage duration (Europe) — Calculation of mean pneumococcal carriage
1347	duration for children under 5 years old in European settings.
1348	
1349	Table S5. Pneumococcal morbidity — Calculation of the annual number of pneumococcal
1350	pneumonia cases in children under 5 in Europe and Kenya.
1351	
1352	Table S6. Carriage duration (Kilifi) — Calculation of mean pneumococcal carriage
1353	duration for children under 5 years old in Kilifi, Kenya.
1354	
1355	Table S7. Priors for model fitting — Table describing prior distributions assumed for
1356	fitted model parameters.
1357	
1358	Table S8. MCMC diagnostics — Widely Applicable Information Criteria (WAIC), Leave-
1359	One-Out Information Criteria (LOOIC), effective posterior sample size and Gelman-
1360	Rubin diagnostics for Bayesian inference model fitting using Markov chain Monte Carlo.
1361 1362	