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Cause-specific or relative survival setting to estimate population-based net survival from cancer? An empirical evaluation using women diagnosed with breast cancer in Geneva between 1981 and 1991 and followed for 20 years after diagnosis

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Abstract

Background.
Both cause-specific and relative survival settings can be used to estimate net survival, the survival that would be observed if the only possible underlying cause of death was the disease under study. Both resulting net survival estimators are biased by informative censoring and prone to biases related to the data settings within which each is derived. We took into account informative censoring to derive theoretically unbiased estimators and examine which of the two data settings was the most robust against incorrect assumptions in the data.

Patients and methods.
We identified 2,489 women in the Geneva Cancer Registry, diagnosed with breast cancer between 1981 and 1991, and estimated net survival up to 20-years using both cause-specific and relative survival settings, by tackling the informative censoring with weights. To understand the possible origins of differences between the survival estimates, we performed sensitivity analyses within each setting. We evaluated the impact of misclassification of cause of death and of using inappropriate life tables on survival estimates.

Results.
Net survival was highest using the cause-specific setting, by 1% at one year and by up to around 11% twenty years after diagnosis. Differences between both sets of net survival estimates were eliminated after recoding between 15% and 20% of the non-specific deaths as breast cancer deaths. By contrast, a dramatic increase in the general population mortality rates was needed to see the survival estimates based on relative survival setting become closer to those derived from cause-specific setting.

Conclusion.
Net survival estimates derived using the cause-specific setting are very sensitive to misclassification of cause of death. Net survival estimates derived using the relative-survival setting were robust to large changes in expected mortality. The relative survival setting is recommended for estimation of long-term net survival among patients with breast cancer.
Introduction

Net survival is defined as the survival that would be observed if the only possible underlying cause of death was the disease under study[1]. This definition of survival probability is of particular interest since it is not influenced by changes in mortality from other causes and therefore allows accurate evaluation of survival from the disease, essential for cancer control.

Two main approaches have been developed to estimate net survival, each requiring different data settings and assumptions. First, the cause-specific approach, which requires a data setting with reliable individual information on the underlying cause of death. Thus, only deaths from the cancer under study are defined as events whilst others are censored. Second, the relative survival approach[2] compares the overall survival of a cohort of patients to that which they would have experienced if they had had the same mortality experience of the general population from which they were drawn. This approach requires a different data setting, where mortality data about the population from which the cancer patients are drawn is available. Information about the cause of death is not required and we assume that the cancer-specific mortality included in the overall mortality is negligible compared to the overall mortality.

Both approaches are prone to a bias called informative censoring[3]. This is where the assumption of independence between the censoring process and the occurrence of the event (death) does not hold. For instance, an older patient is more likely to die from other causes than the disease under study than a younger patient. Thus, the older patients are more likely not to experience the death from cancer of interest simply because of their older age. The censoring process is therefore dependant on age and becomes informative. To take into account this bias, Robins[4] and Satten[5] proposed to weight the observed data by the inverse of the probability of not dropping out of the risk set, in order to find a cohort which would have been seen without the withdrawals. Pohar Perme[6] used this idea to propose an unbiased estimator of net survival within the relative survival setting.

As long as informative censoring is accounted for appropriately, both cause-specific and relative survival approaches derive theoretically unbiased estimators of net survival. However these estimators are prone to biases related to the data settings within which each is derived. These biases are independent of the method of estimation.

In the cause-specific data setting, what defines a cancer-related death versus a death from another cause is reliant upon the judgment of the person extracting the information and often prone to misclassification. Several studies have described this bias as being non-negligible[7–14]. For this reason the relative survival method has generally been preferred to estimate net survival with population-based data[15, 16]. However, within the relative survival data setting non-comparability between the cohort of patients and the general population[17] life tables used can also lead to bias. If a factor is differently distributed between patients and the general population, the resulting expected mortality of the cohort will be incorrectly estimated[18]. For instance, patients with lung cancer are more often smokers compared with the general population. Their expected mortality is therefore underestimated as they are more likely to die from other causes than the general population.[19]
long term, this under-estimation may be balanced by the selection process over time of the more robust patients, who may die less than the general population[20]. This may impact net survival estimates[21]. Similarly, several factors can be associated with both cancer mortality and other diseases and lead to non-comparability between observed and expected mortality.

Our objective was to compare the two data settings, cause-specific and relative survival, when estimating long-term net survival. Both are subject to bias as described above; either misclassification of the cause of death or use of inappropriate life tables. We first derived theoretically unbiased estimators by using weights for both approaches, which took into account informative censoring. We then performed two sensitivity analyses in order to examine which of the two data settings was more robust against incorrect assumptions. We used each estimator as a reference for the other in order to evaluate the impact on the net survival estimates (Table 1).

We used data from the Geneva Cancer Registry which holds high quality data on cancer patients collected since 1970. This enabled us to evaluate the effect of these biases on long-term net survival. Furthermore, it afforded a privileged situation for estimating net survival within the cause-specific setting as information on cause of death had been independently verified.
Material and methods

Data

The data were provided by the Geneva Cancer Registry.

The Geneva Cancer Registry collects information on incident cancer cases from various sources, including hospitals, laboratories and private clinics, all requested to report new cancer cases. Trained registrars systematically extract information from the medical records and conduct further investigation in the case of missing key data. The registry regularly assesses survival, taking as the reference date the date of confirmation of diagnosis or the date of hospitalization (if it preceded the diagnosis and was related to the disease). In addition to passive follow-up (standard examination of death certificates and hospital records), active follow-up is performed yearly using the files of the Cantonal Population Office who maintain a register of the resident population. The cause of death is validated or revised from death certificates by registrars using all available clinical information. Autopsy reports, letter at death written by general practitioners and all patients’ medical notes are used for the assessment of the revised cause of death. The treatment can therefore be considered as breast cancer death when information is found about it being part of the morbid events leading directly to death.[22] We included all women diagnosed with an invasive primary breast cancer between 1981 and 1991. These women have all been followed-up for a minimum of 20 years, and the last date of follow-up was 31st December 2011.

Statistical methods

Informative censoring

Informative censoring in a cohort of cancer patients is a differential selection process which affects the likelihood of the event of interest being observed. Different strategies have been derived for each data setting and are able to take into account informative censoring when estimating net survival (Appendix A).

The recently proposed Pohar-Perme[6] estimator enables informative censoring to be accounted for in the relative survival data setting, using weights calculated from the expected mortality of each cancer patient according to their individual characteristics. Expected mortality is derived from life tables for the general population from which the cancer patients are drawn and were previously smoothed.

In the cause specific setting, we used a similar strategy to weight the net survival estimator. We derived the weights using the cancer patient data and validated cause of death. We considered that the expected mortality of the cancer patients would be the same as the mortality rate from other causes of death than breast cancer amongst the cancer patients. We fitted a Poisson regression model to the cancer patient data where we considered death from a cause other than breast cancer as the event of interest. We adjusted on age at death and year of death. We used the model to derive expected mortality by age and year. We then used this set of rates to weight the breast-specific mortality hazard, in order to derive net survival estimates.
Potential biases related to the cancer data

In the relative survival setting, the potential bias of interest is related to the comparability between the cancer patients and the general population. An under-estimation of the expected survival would lead in an over-estimation of the net survival. On the contrary, an over-estimation of the expected survival would result in an under-estimation of net survival (Table 2).

In the cause-specific setting, the potential bias of interest is related to the accuracy of the classification of the cause of death. There are two possibilities; the proportion of breast cancer among the deceased patients is either over- or under-reported. If some non-specific deaths are misclassified as breast cancer deaths, the number of deaths from breast cancer is inflated. Net survival is therefore underestimated. Similarly, net survival is over-estimated when some breast cancer deaths are misclassified as non-breast cancer deaths (Table 2).

Sensitivity analyses

In order to investigate the biases related to each data setting we performed two sensitivity analyses (Table 3).

We defined the baseline situation as the estimation of net survival using the revised and/or validated cause of death in the cause-specific data setting, and the official Geneva life table in the relative survival data setting. We considered that both of these methods derive theoretically unbiased estimates of net survival.

We observed that in the baseline situation (Figure 1) net survival estimates derived using cause-specific data setting were higher than the relative survival data setting. We therefore concentrated our sensitivity analysis on two of the four potential biases to evaluate how this difference could have arisen (①and ④Table 2).

In scenario A, we evaluated whether the suitability of the life table in the relative survival data setting might be responsible for the difference observed (④Table 2). Mortality rates of the general population are only available by age, sex and calendar period in the Geneva canton. Nevertheless, other socio-demographic factors also influence the probability of death for an individual cancer patient. If the life table used in the relative survival setting does not accurately reflect the background risk of death of the cancer patient cohort, biased estimates of survival may result. This can happen, for example, because women with breast cancer tend to be more affluent than the overall population and these affluent women have a lower expected mortality rate than the population of women overall.

Deprivation information about cancer patients is available in three categories in the Geneva Cancer Registry (high, medium and low socio-economic position) but the expected mortality available is not detailed by deprivation. We therefore employed the rate ratios for the first, third and fifth quintiles of
deprivation (derived from the England and Wales mortality rates for deprivation quintiles[23]) to build deprivation-specific expected mortality for the three socio-economic groups in the Geneva data. This generated a conservative situation because the differences between these quintiles in the English and Welsh data are likely to be greater than the (unknown) ratios between the three socio-economic groups in Geneva. This resulted in a substantially increased risk of death from other causes for the low socio-economic group and decreased risk for the high socio-economic group (Figure 2). These deprivation-specific life tables were then used to estimate net survival up to 20 years after diagnosis (scenario A1).

We further evaluated the degree to which expected mortality needed to increase in order to eliminate the difference we observed between the two estimators. We applied the life table for lowest socio-economic group (who have the highest mortality rates) to all the women in the data and estimated net survival up to 20 years after diagnosis (scenario A2).

We computed the difference between the baseline estimator of net survival using the cause-specific data setting and the relative survival estimators in scenario A1 and A2. Differences were smoothed by running a weighted non-parametric regression on time after diagnosis [24].

In scenario B, we considered misclassification of cause of death as the potential cause of the difference (Table 2). Since the cause-specific data setting produced the higher of the two estimations, we considered only the situation in which breast cancer deaths had been misclassified as non-specific deaths. In this situation net survival calculated using the cause-specific approach would decrease.

We randomly re-attributed the cause of death variable from non-breast cancer to breast cancer for 10, 15, 20 and 25 per cent of the deceased patients (scenarios B1, B2, B3 and B4, respectively). We iterated this re-attribution 100 times and derived the mean cause-specific net survival up to 20 years for each scenario. The confidence interval was derived using the 95% coverage. The proportion of deaths due to breast cancer among deceased patients varied from 49.7% in the baseline situation to 62.2% in scenario B4 (table 4).

We computed the difference between the baseline estimator of net survival using the relative survival data setting and the cause-specific estimators for scenarios B1, B2, B3 and B4 respectively. Differences were smoothed by running a weighted non-parametric regression on time after diagnosis [24].
Results

The final cohort was comprised of 2,489 women diagnosed with an invasive breast cancer between 1981 and 1991 in Geneva, Switzerland.

Figure 1 shows the baseline situation where net survival estimator using the cause-specific setting was higher than the estimation using relative survival setting for all of the 20 years of follow-up.

The absolute difference between the two estimators increased with time after diagnosis from 1% at one year to 10.8% at 20 years. It remained less than 3% during the first ten years of follow-up (2.4% at 10 years) and started to increase more dramatically from 13 years onwards (Figure 1).

In scenario A1, where deprivation-specific life tables were applied, we observed a smaller but still substantial difference between the estimators (Figure 3). By contrast, the smoothed difference between the two different net survival estimators derived for scenario A2 (use of life tables of the most deprived population) was close to 0 during most of the first ten years after diagnosis (Figure 3).

Scenarios B1 to B4 correspond respectively to the re-allocation of 10, 15, 20 and 25% of deaths from non-breast cancer to breast cancer (Figure 4). As the proportion of re-allocation increased, the difference between the cause-specific approach and the baseline estimate derived within the relative survival data setting decreased, even turning negative. When 15-20% of the deaths were reallocated, the difference was close to zero. This suggested that with this level of reallocation the cause-specific approach and the relative survival approach used in the baseline situation derived a very similar estimate of net survival up to 10 years after diagnosis. Looking at results after 10 years, the two net survival estimators derived similar estimations when 25% of deaths were reallocated.
Discussion

Net survival is the survival that would be observed in a hypothetical world where the only possible underlying cause of death is the disease under study. This study is the first to account for informative censoring in the estimation of net survival in both cause-specific and relative survival data settings, allowing an accurate comparison of two unbiased estimators of net survival. Theoretically, both methods should give the same estimates of net survival. However, both net survival estimates are prone to biases related to the data and their specific assumptions. Differences in the estimates can be attributed to (i) incorrect expected mortality due to inadequate life tables in the relative survival data setting, or (ii) errors in the cause of death for some patients in the cause-specific data setting. We have evaluated these two possibilities using data on breast cancer patients whose cause of death has been independently validated, and who have been followed for 20 years after their diagnosis.

In the cause-specific setting, weights, estimated using the mortality hazard specific to the other causes of death from the cancer registry data, were applied to tackle informative censoring and estimate theoretically unbiased net survival. Although these internal weights were derived from a model, they may have been unstable due to small numbers of deaths in this fairly small breast cancer population. We thus also derived the weights using the expected mortality from the general population life tables (therefore similar as those used with the relative survival setting). Both weighting approaches gave very similar results, confirming the strength of the cause-specific setting estimator. We assumed that the weighted net survival estimator in the cause-specific setting was theoretically unbiased and equivalent to the Pohar Perme approach. However, simulation-based work is needed to assess its performance.

We observed that the cause-specific approach gave higher estimates of net survival compared to the relative survival approach (Figure 1). Moreover, the absolute difference between the two estimators increased with time since diagnosis up to 2.5% at 10 years after diagnosis and over 10% at 20 years. This enabled us to consider only two (① and ④, Table 2) out of the four potential biases related to the data setting. Indeed, we did not evaluate option ② or ③. Option ② considers the situation in which net survival is over-estimated because of under-estimated expected survival. This situation is unlikely insofar as cancer survivors are often prone comorbidities and are therefore no less likely to die than the general population, even if at longer term, the situation may be reversed, with the more robust patients being selected [25] [26]. Option ③ describes the situation in which net survival is under-estimated because deaths not due to breast cancer are mistakenly classified as breast cancer deaths. It is however more likely that the true number of breast cancer deaths is underestimated because deaths caused indirectly by breast cancer may be misclassified.

We first estimated net survival in the relative survival setting using different life tables to evaluate whether non-comparability between the general population and the cohort of patient under study compromises the estimation of net survival. In our study, we stratified the life table on deprivation (scenario A1) and the results showed that the net survival estimation was not substantially altered by this. In scenario A2, we noticed that a very large increase in the mortality rate was required (30% for a
50 year old woman) before the net survival estimated in the relative survival setting reached the net survival estimated in the cause-specific setting during the first 8 years after diagnosis. Such changes seem quite unreasonable at a population level. Net survival in the relative survival setting appeared therefore to be robust to inaccuracies in the underlying mortality rate.

The second sensitivity analysis showed that the level of misclassification could be relatively small to observe a large change in net survival. Indeed, recoding only 10% of the non-specific deaths led to a large decrease of the net survival using the cause-specific settings. The estimator of net survival derived with cause-specific method proved therefore to be relatively sensitive to the allocation of the cause of death. Recoding 15-20% of deaths from other causes to breast cancer resulted in the convergence of the net survival estimates in both settings. We have previously shown that a review of clinical files resulted in cause of death being revised for 9 per cent of women with breast cancer in the Geneva Cancer Registry data[22]. In the current study, 20% of the non-specific deaths represented 171 cases out of the 1700 deceased patients. As such, survival estimates are likely to be biased by the misclassification of a relatively small number of deaths that are indirectly related to breast cancer (for instance; side effects of treatment or suicide). The fact that the proportion of reallocation required to reduce the survival difference to zero increased after 10 years after diagnosis (from 10% to 15%) lends weight to this argument insofar that allocating breast cancer as an underlying cause of death is less probable with increasing time since diagnosis.

Taken together, these results suggest that survival derived with the cause-specific approach provides a very sensitive estimator, likely to be an overestimate of true net survival. On the contrary, survival derived with the relative survival approach is likely to be closer to the actual net survival of the patient cohort insofar as it is very robust to changes to the expected rate of death. This is especially true with increasing time after diagnosis.

Our study has considered only women with breast cancer. Breast cancer patients are not, however, representative of patients with cancer at different localisations. The proportions of specific deaths and age have a large impact in biases related to net survival. Future work will test the repeatability of our analyses on other cancer sites by different age groups. Preliminary results on cancers of colon-rectum, lung and on melanoma suggested results consistent with those provided by this study.

A dramatic increase in long-term survivors has been observed over the last few decades as a result of screening programs, more precise diagnostic tools and developments in treatment protocols.[27]. In the future a particular interest will be given to long-term net survival estimation, especially among younger patients.

Our results suggest that, when analysing routinely collected population-based data, the relative survival setting is likely to derive more accurate estimates of net survival, and that the cause specific setting is vulnerable to misclassification bias, particularly in the long-term. The relative survival setting is therefore highly recommended when estimating net survival with population-based data.
Table 1. Description of the two data settings available for the estimation of net survival.

Table 2: Potential biases related to data settings when estimating net survival.

Table 3. Description of the sensitivity analyses performed in order to check the extent of biases related to the data settings.

Figure 1. Net survival estimators in the baseline situation using both cause-specific and relative survival settings.

Figure 2. Geneva general population mortality rates by age for year 1991. Comparison between the baseline situation and scenarios A.

Table 4: Deaths distribution among female breast cancer patients diagnosed in Geneva between 1981 and 1991 according to scenarios.

Figure 3. Smoothed differences between the net survival estimators when informative censoring is taken into account: Cause-specific setting in the baseline situation vs. Relative survival setting in baseline situation, scenario A1 and scenario A2.

Figure 4. Smoothed differences between the net survival estimators when informative censoring is taken into account: Cause-specific setting in the baseline situation, scenarios B1, B2, B3 and B4 vs. Relative survival setting in the baseline situation.

Supplementary material

Appendix A. Description of net survival estimation when taking into account the theoretical bias of informative censoring.
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Disclosure
The authors have declared no conflict of interest.
References


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<th>NET SURVIVAL</th>
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<tr>
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<td>Informative censoring</td>
<td>Cause-specific</td>
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<td>Misclassification of the cause of death</td>
<td>Relative survival</td>
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<td>Non comparability between the cohort and the general population</td>
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<td>Weight the net survival estimator with the expected mortality</td>
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<td>Use the cancer data to estimate the expected mortality</td>
<td>Use the expected mortality derived from general population expected mortality</td>
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<td>Modify the expected mortality rates of the general population</td>
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<td><strong>Under-estimation</strong></td>
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<td>% of BCD in the data</td>
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BCD: Breast Cancer Deaths  
$E_p$: Expected survival of the general population  
$E_c$: Expected survival of the cancer patients
### Table 3

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<th>Baseline situation</th>
<th>Scenario</th>
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<td>Relative survival</td>
<td>Official Geneva life table</td>
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<td>Life table of the most deprived</td>
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<td>% of deaths reallocated†</td>
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<td>Other cause of death</td>
<td>Total number of deaths</td>
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<tr>
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<tr>
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<td>(N^*)</td>
<td>%*</td>
<td>(N^*)</td>
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<td>Scenario B2 15%</td>
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<td>Scenario B3 20%</td>
<td>1015</td>
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<td>Scenario B4 25%</td>
<td>1058</td>
<td>62.2</td>
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† Percentage of cases with non-specific cause of death randomly recoded as breast cancer.

*The numbers \((N)\) and percentages \(\%\) given are an average of the 100 iterations for scenarios B1, B2, B3 and B4.
## NET SURVIVAL

### Net survival estimator
\[ \hat{\lambda}_e(t) = \int_0^t \frac{dN^e(u)}{Y^e(u)} - \int_0^t \frac{\sum_{i=1}^n I(u) dN_i(u)}{Y^e(u)} \]

- Estimated from the cancer data
- Estimated from the general population life table

### Bias
Informative censoring

<table>
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<th>Cause-specific</th>
<th>Relative survival</th>
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</thead>
<tbody>
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<td>Event considered</td>
<td>Specific deaths</td>
<td>All deaths</td>
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### Weights \( W \)
\[ X_i^w = \frac{X_i(t)}{S_{P_i}(t)} \]
where \( S_{P_i}(t) \) is the expected survival of individual \( i \) at time \( t \)

### Origin of the weights
Life table of the general population
Cancer data
Life table of the general population

### Unbiased estimator of net survival
\[ \hat{\lambda}_e(t) = \int_0^t \frac{dN^w(u)}{Y^w(u)} \]

### Pohar Perme estimator:
\[ \hat{\lambda}_e(t) = \int_0^t \frac{dN^w(u)}{Y^w(u)} - \int_0^t \frac{\sum_{i=1}^n I(u) dN_i(u)}{Y^w(u)} \]

### Corresponding curve in figure 1
- I
- II
- III

<table>
<thead>
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</tr>
<tr>
<td>W</td>
<td>weight</td>
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<tr>
<td>Y</td>
<td>number of patients at risk up to ( t )</td>
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<tr>
<td>N</td>
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<td>N_i</td>
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<tr>
<td>A_e(t)</td>
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Figure 1

Net survival using:

- **I)** Cause specific setting. Weights from LT.
- **II)** Relative survival setting.
- **Difference between I and II**
Figure 3

Smoothed difference between the two net survival estimators (%)

- Baseline situation
- Scenario A1 (life table adjusted for deprivation)
- Scenario A2 (most deprived life table)

Years since diagnosis

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Click here to download high resolution image
Figure 4
Click here to download high resolution image